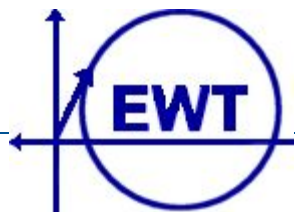


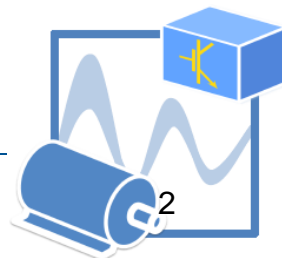
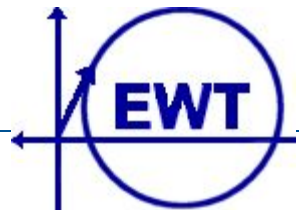
Leistungselektronik – Grundlagen und Standardanwendungen SS 2012

DC/DC Converter Fundamentals

Prof. Hans-Georg Herzog
Technische Universität München
Elektrische Energiewandlungstechnik

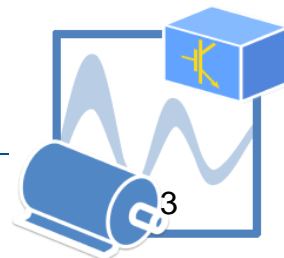
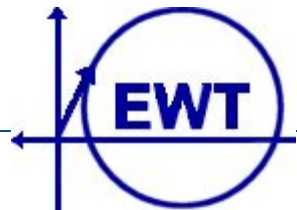


1. Overview on DC/DC Converter
2. One-Quadrant Converter
 - Buck Converter
 - Boost Converter
 - Buck-Boost Converter
 - Cuk Converter
3. Two-Quadrant Converter
4. Multi-Phase DC/DC Converter

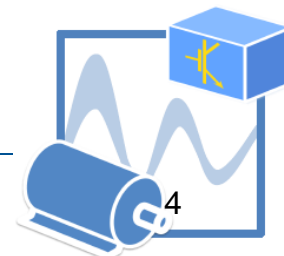
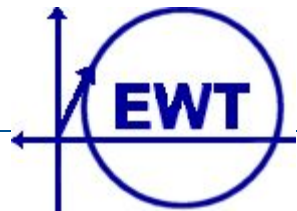
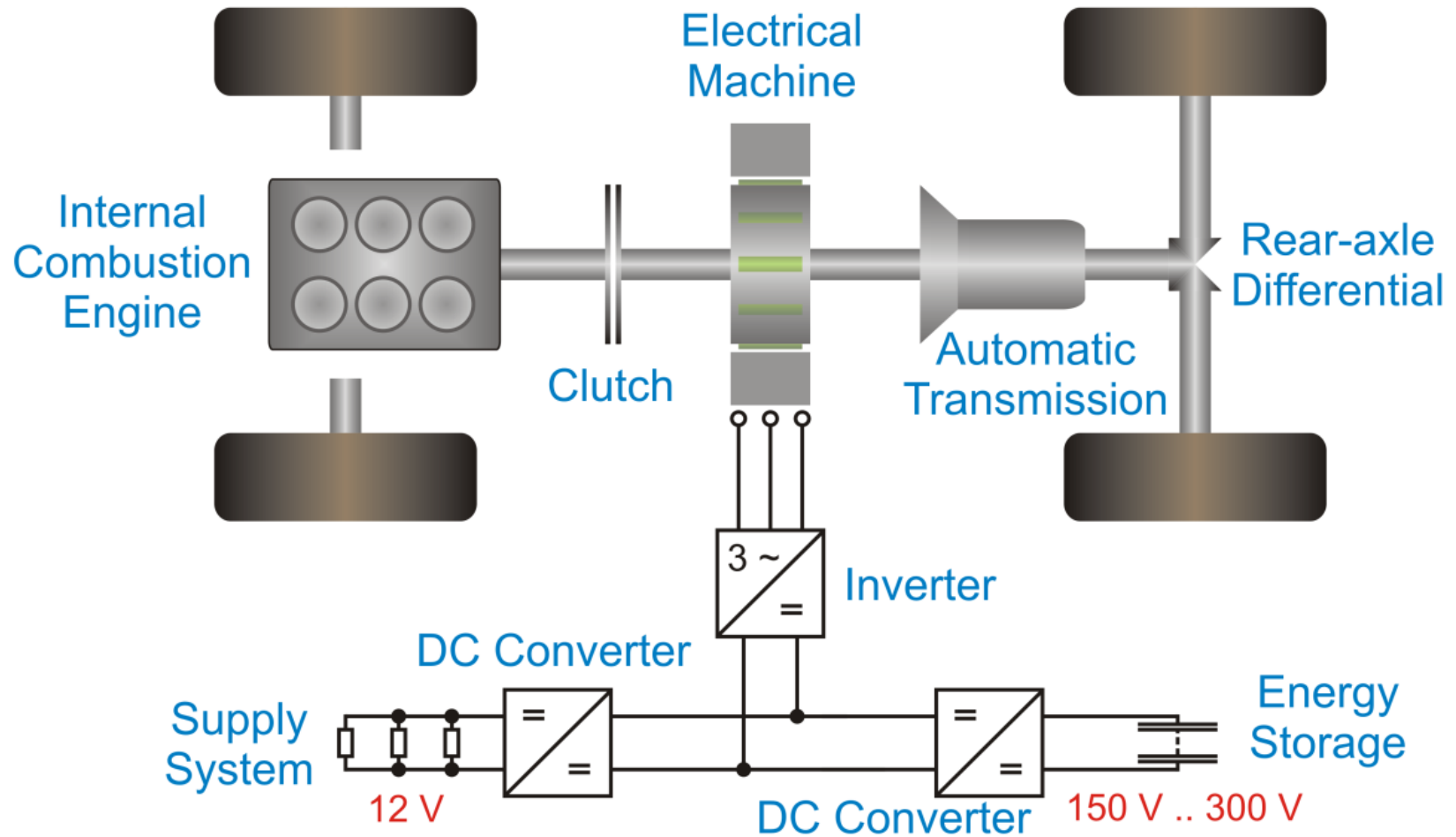


Fields of Application

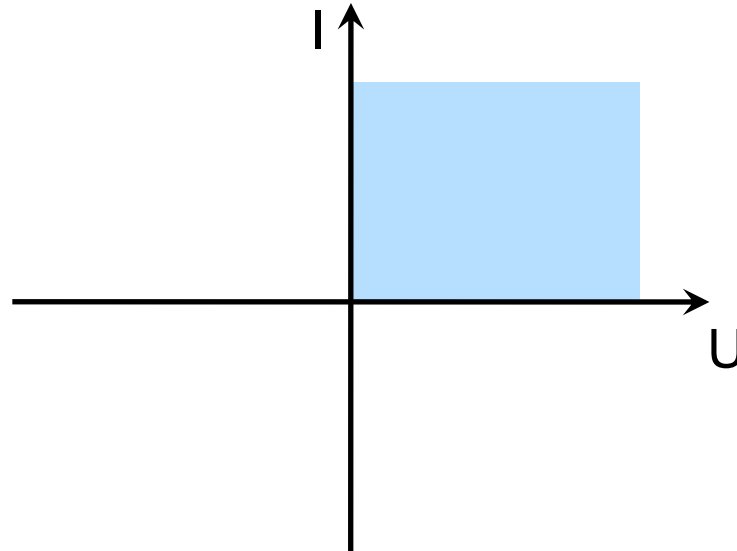
- Switched-Mode Power Supplies ($\leq 300\text{W}$)
 - Supply of μC
 - PC Power Supply
- Automotive (some kW)
 - Coupling of Multi-Voltage On-Board Supply Networks
 - Connection of Energy Storage Devices, Thermo-Electric Generators, Solar Panels, ...
- Controlled DC-Drives (several 10 kW)



Fields of Application in Vehicles

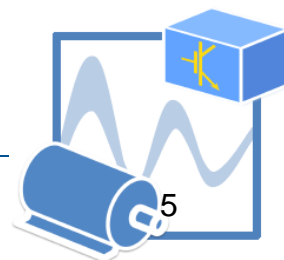
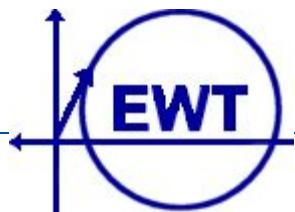


One-Quadrant Converter

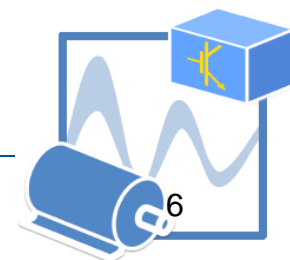
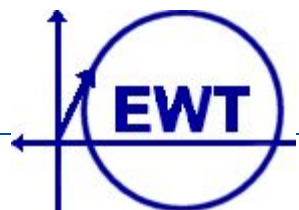
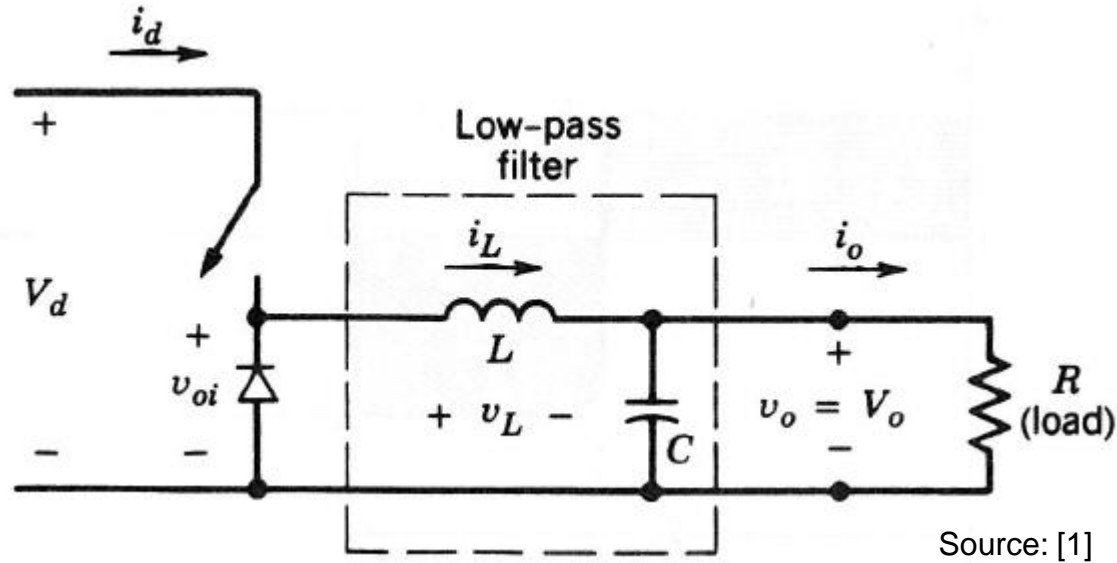


Fields of Application:

- Unidirectional Coupling of Two On-Board Networks
- Connecting Components with Lower Voltage Level to a Higher Voltage On-Board Network



Buck Converter – Principle Circuit

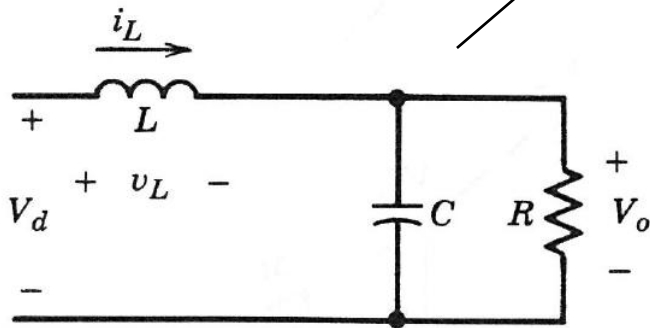
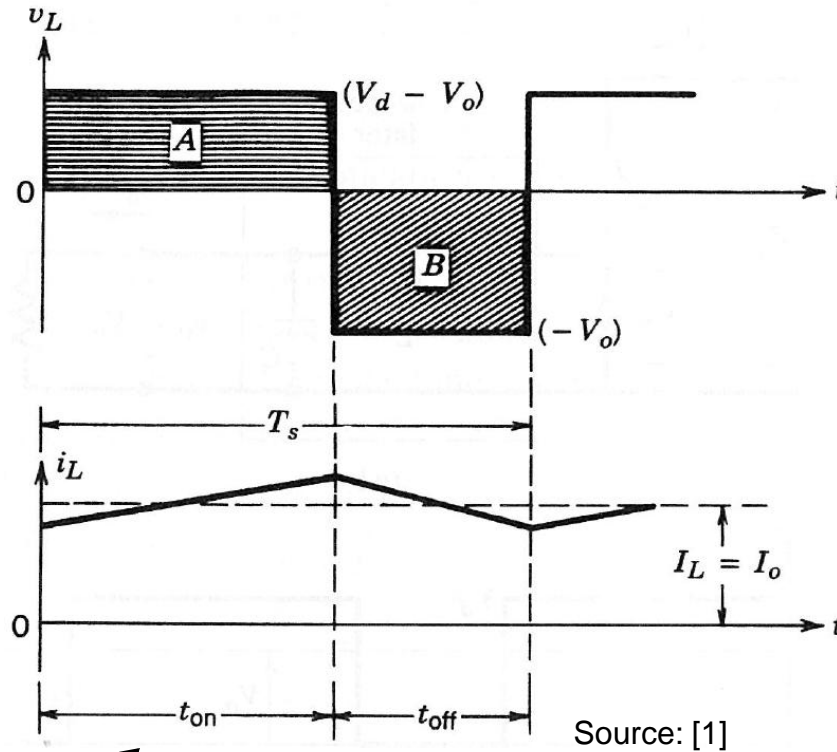


Buck Converter – Switching States

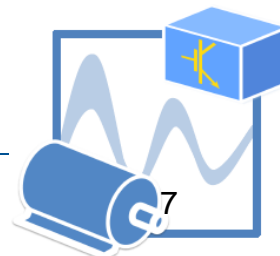
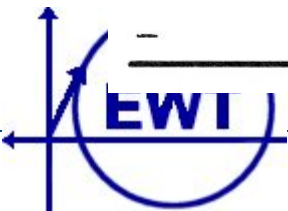
Assumption:

$V_O = \text{const.}$

$T_s = t_{on} + t_{off}$



$$i_L(t) = I_{S,B0} + \frac{V_d - V_0}{L} \cdot t$$

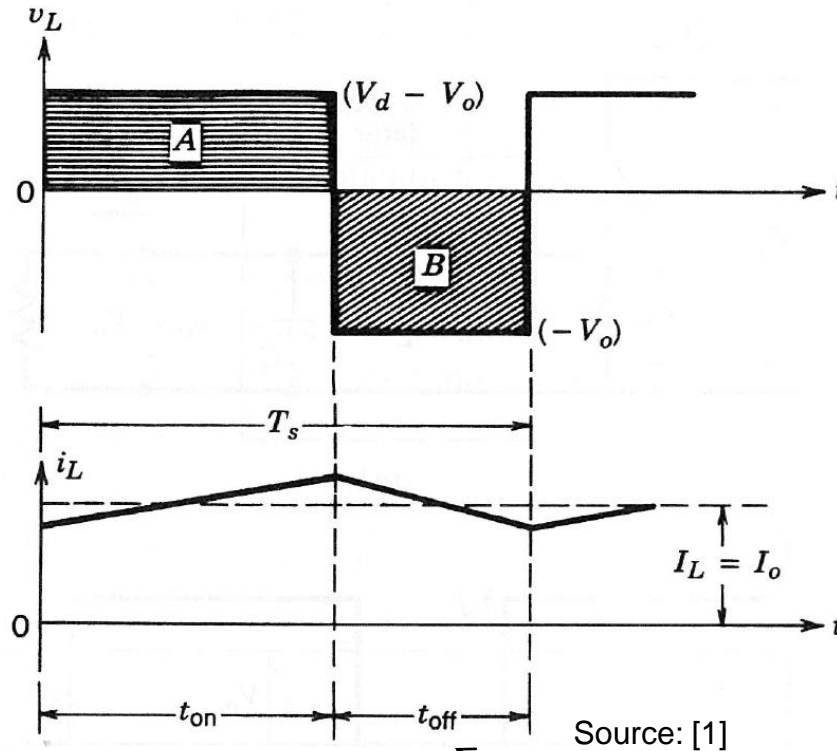


Buck Converter – Switching States

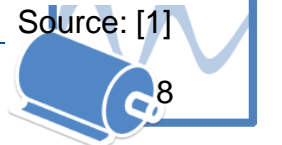
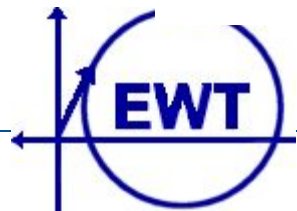
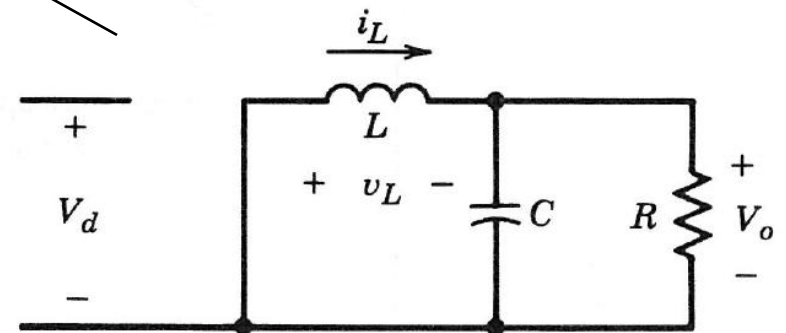
Assumption:

$V_o = \text{const.}$

$T_s = t_{on} + t_{off}$



$$i_L(t) = I_{S,Up} + \frac{(-V_o)}{L} \cdot t$$

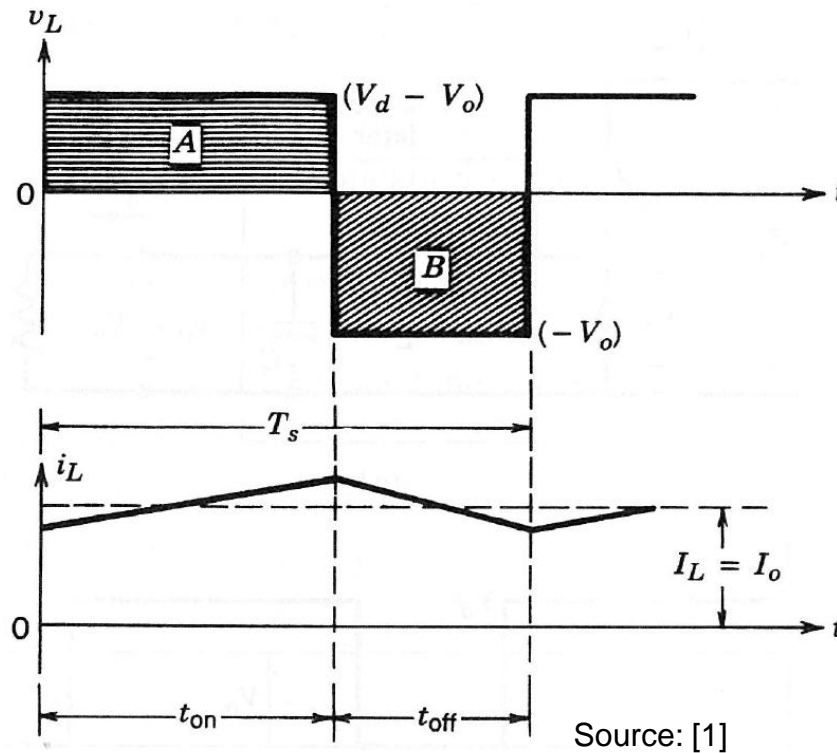


Buck Converter – Switching States

Assumption:

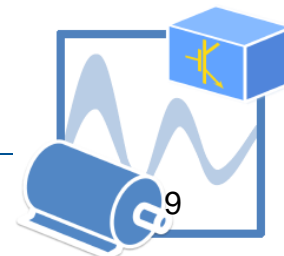
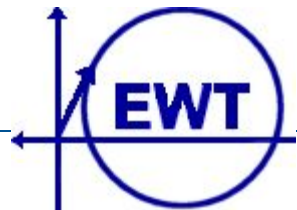
$V_O = \text{const.}$

$T_s = t_{on} + t_{off}$

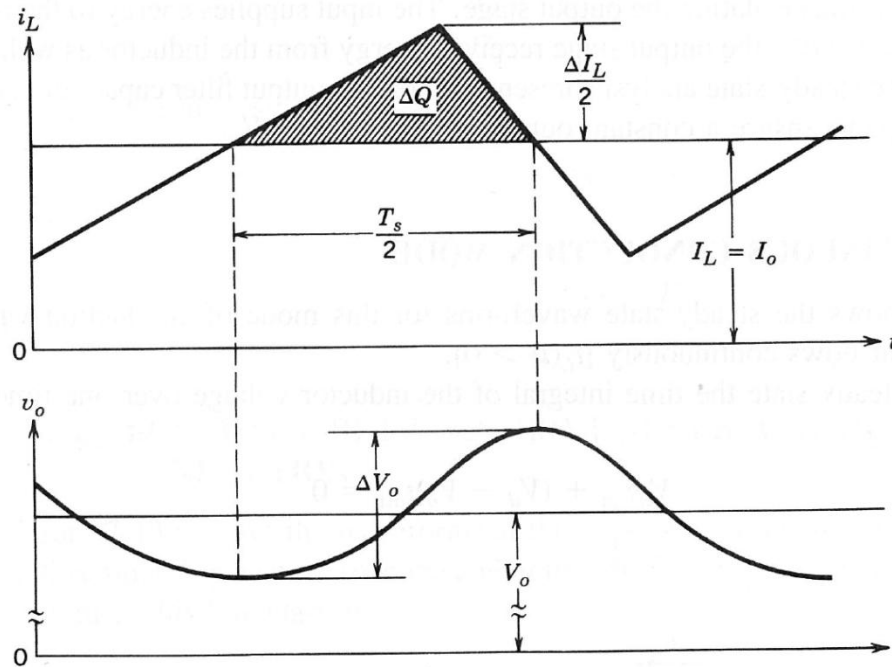


Steady-State: Area A = Area B $(V_d - V_O) \cdot t_{on} = V_O \cdot (T_s - t_{on})$

$$\frac{V_O}{V_d} = \frac{t_{on}}{T_s} = D$$



Buck Converter – Output Voltage

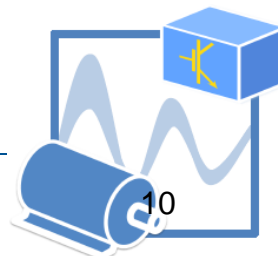


Source: [1]

$$\Delta V_o = \frac{\Delta Q_o}{C} = \frac{1}{C} \cdot \frac{1}{2} \cdot \frac{\Delta I_L}{2} \cdot \frac{T_s}{2}$$

$$\Delta V_o = \frac{T_s^2}{8C} \cdot \frac{V_o}{L} \cdot (1 - D)$$

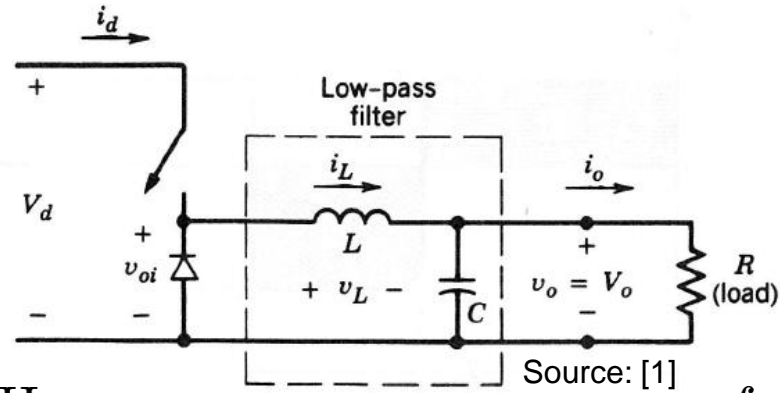
$$\Delta I_L = \frac{V_o}{L} \cdot (1 - D) \cdot T_s$$



Buck Converter – Simulation Results

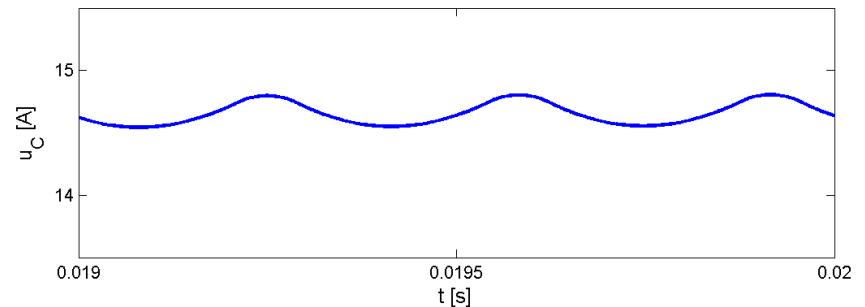
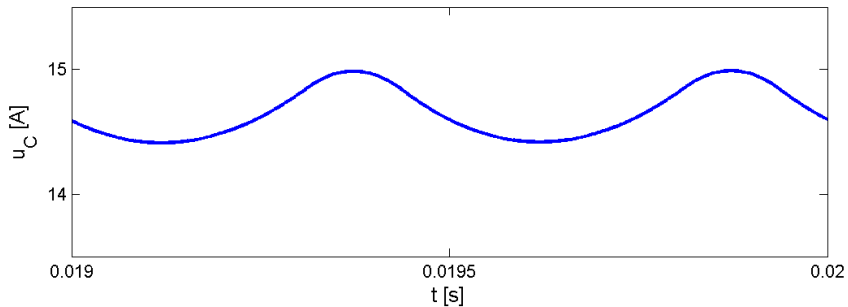
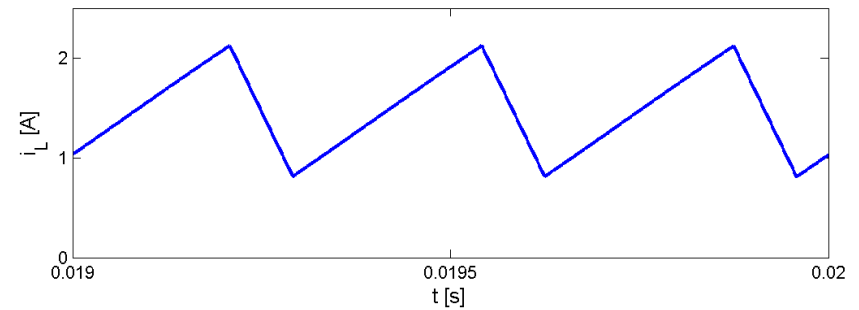
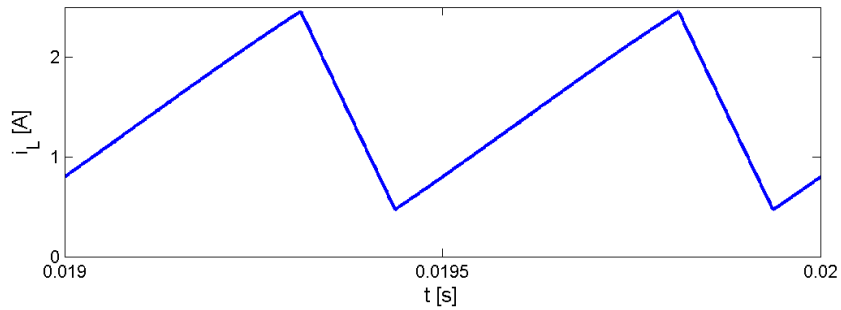
$$V_d = 20 \text{ V}$$

$$D = 0.75$$

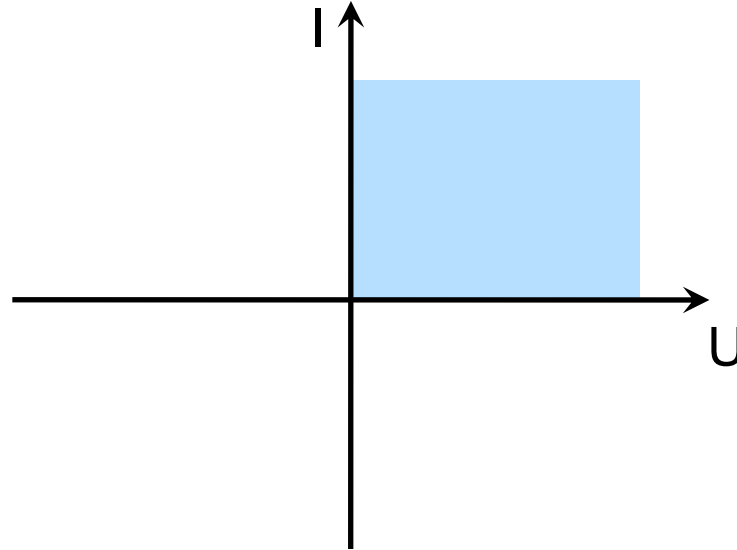


$$f_s = 2 \text{ kHz}$$

$$f_s = 3 \text{ kHz}$$



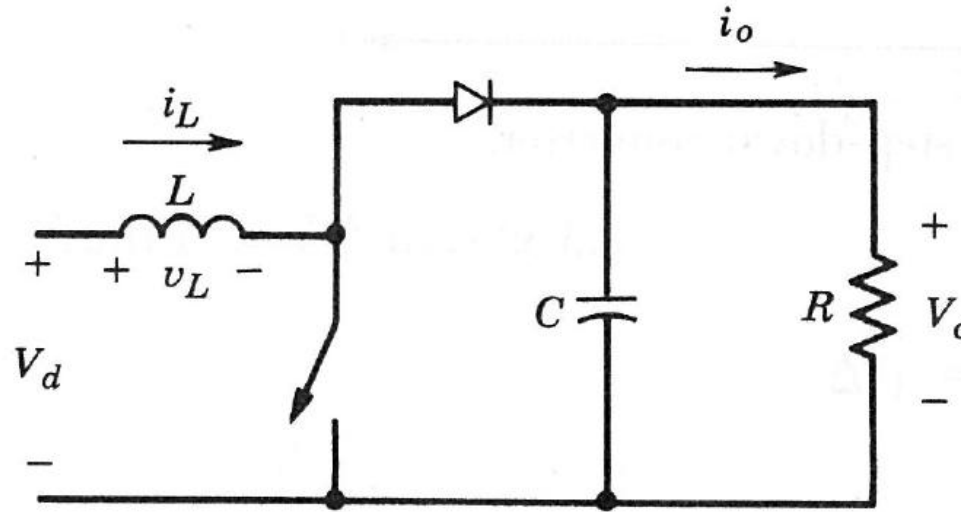
One-Quadrant Converter



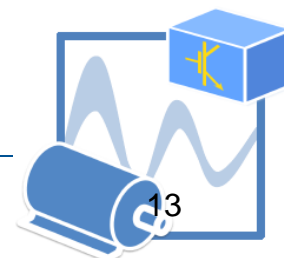
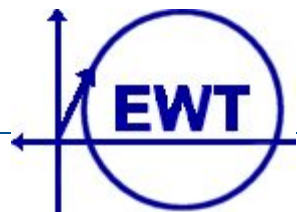
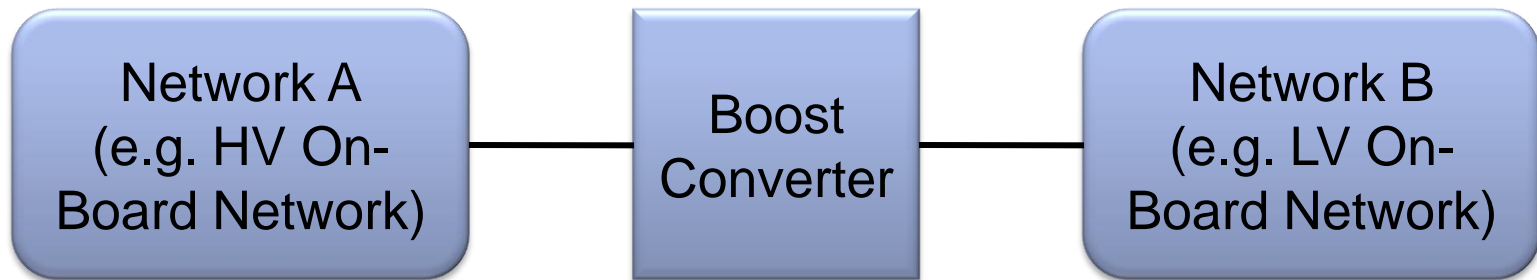
Fields of Application:

- Unidirectional Coupling of Two On-Board Networks
- Connecting Components with Higher Voltage Level to a Lower Voltage On-Board Network

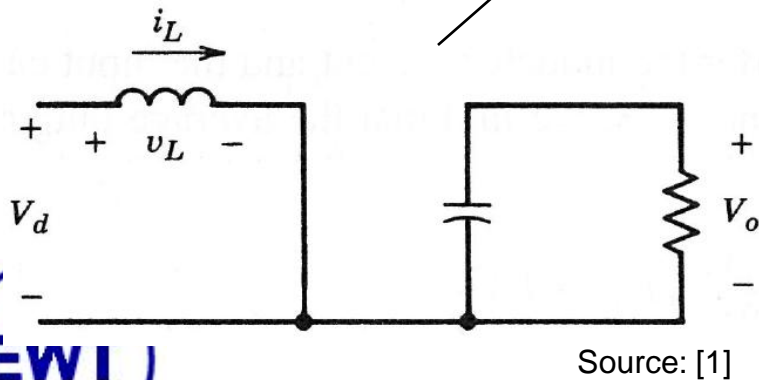
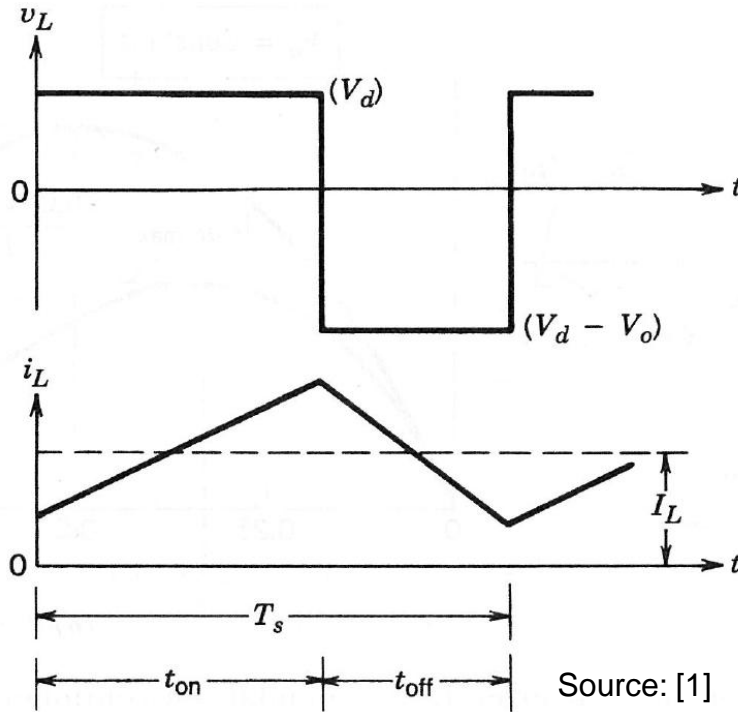
Boost Converter – Principle Circuit



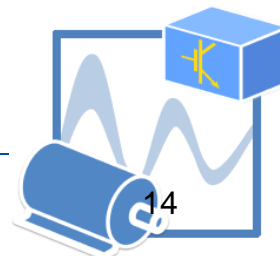
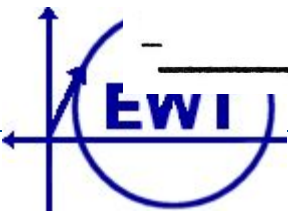
Source: [1]



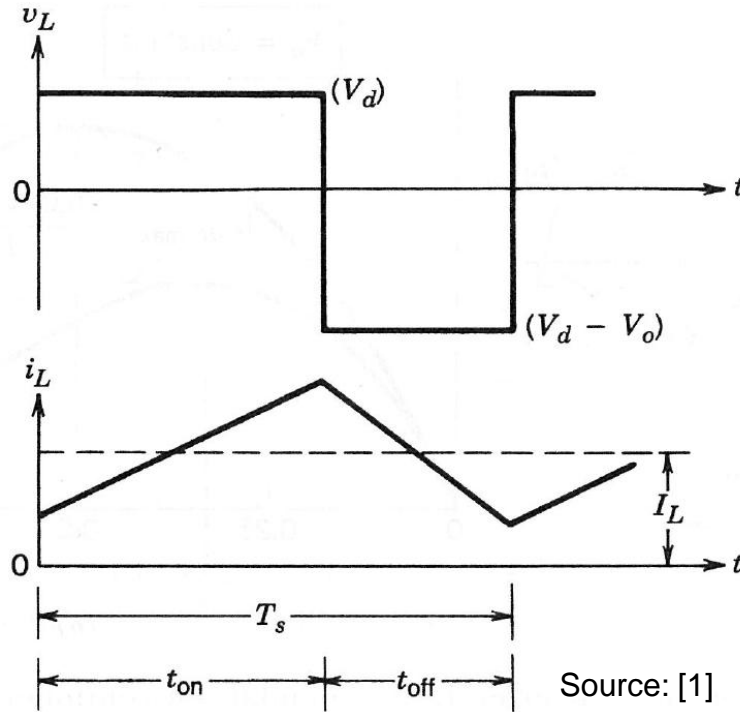
Boost Converter – Switching States



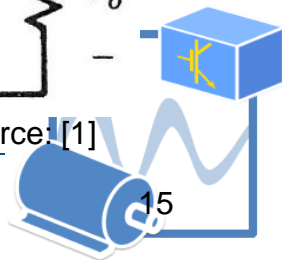
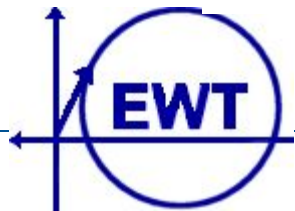
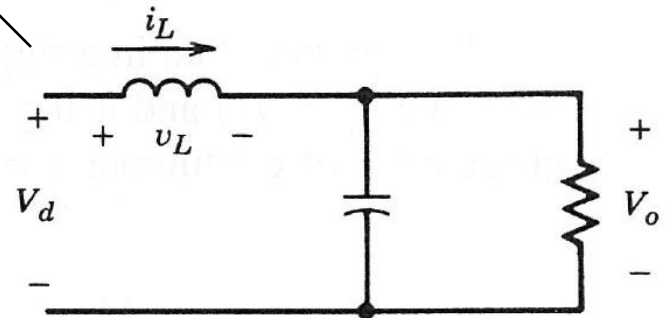
$$i_L(t) = I_{S,Bo} + \frac{V_d}{L} \cdot t$$

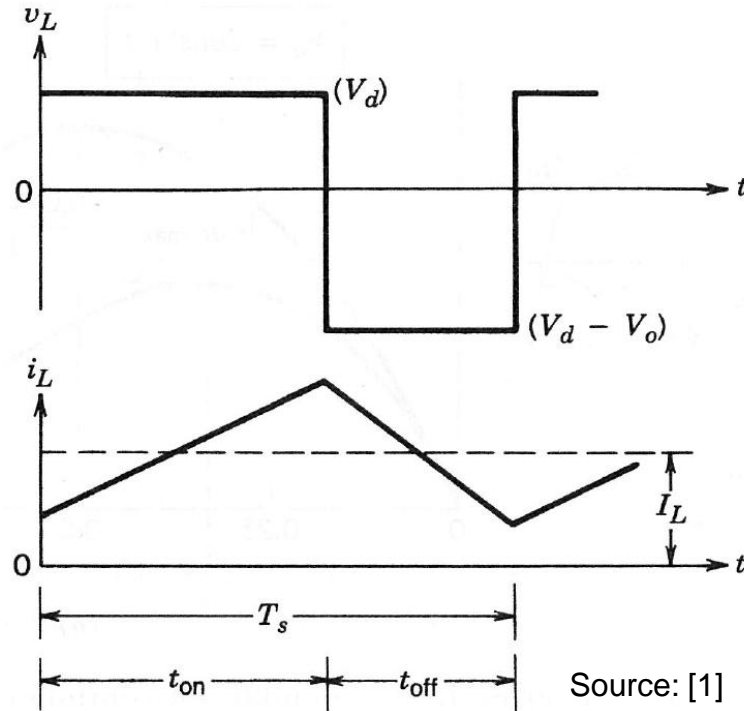


Boost Converter – Switching States



$$i_L(t) = I_{S,Up} + \frac{V_d - V_o}{L} \cdot t$$

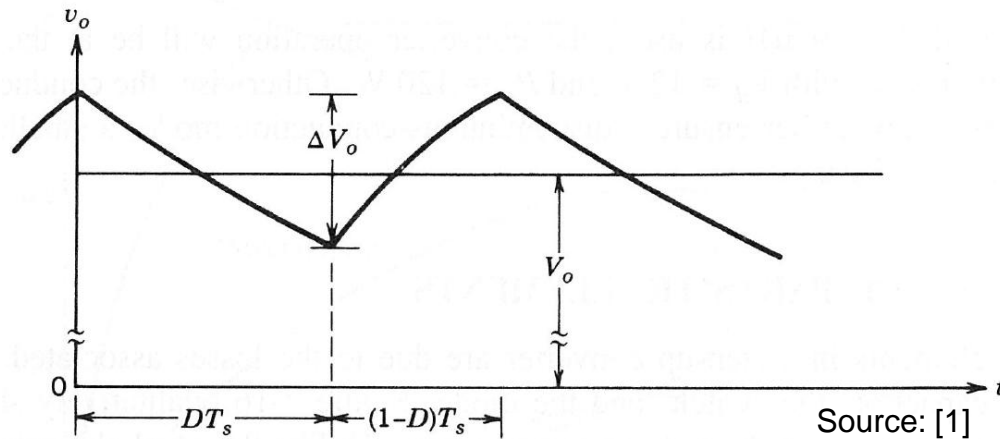
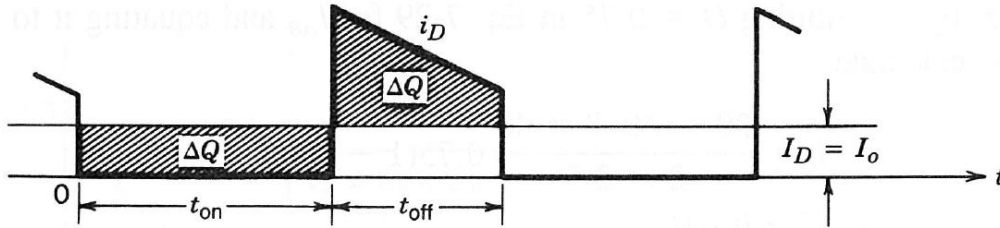




Steady-State: $V_d \cdot t_{on} + (V_d - V_o) \cdot t_{off} = 0$

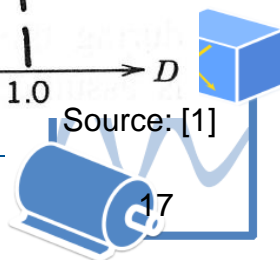
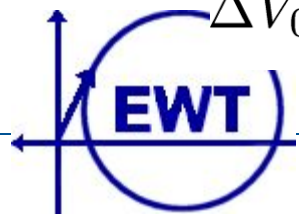
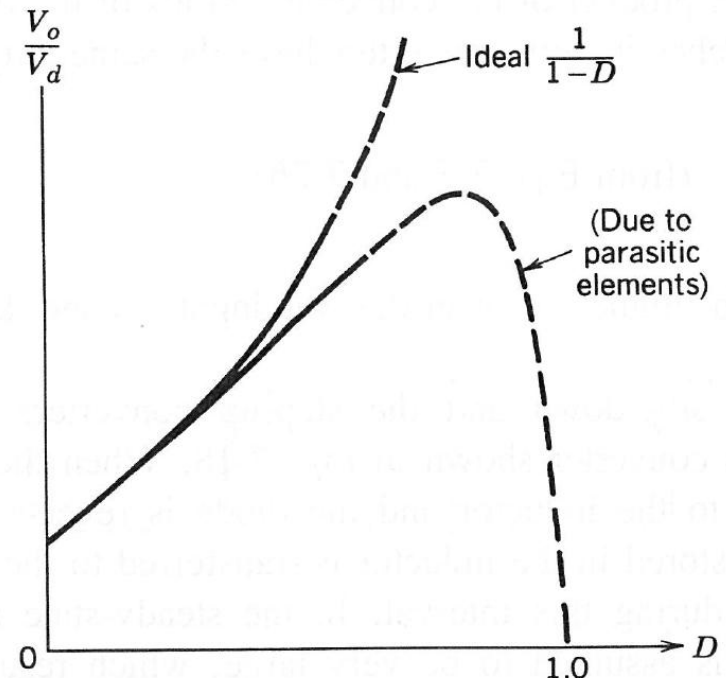
$$\frac{V_o}{V_d} = \frac{T_s}{t_{off}} = \frac{1}{1 - D}$$

Boost Converter – Output Voltage



$$\Delta V_0 = \frac{\Delta Q}{C} = \frac{I_0 \cdot D \cdot T_s}{C}$$

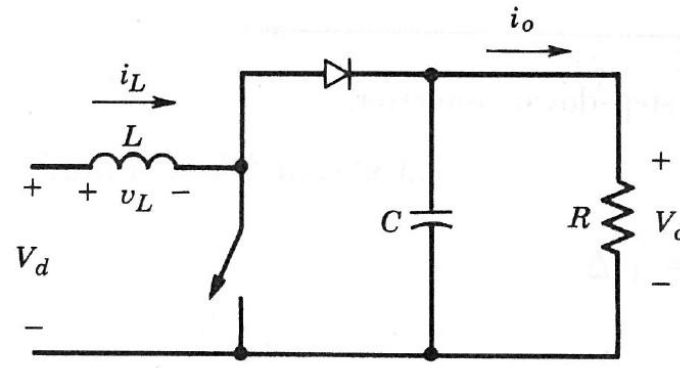
$$\Delta V_0 = \frac{V_0}{R} \cdot \frac{D \cdot T_s}{C}$$



Boost Converter – Simulation Results

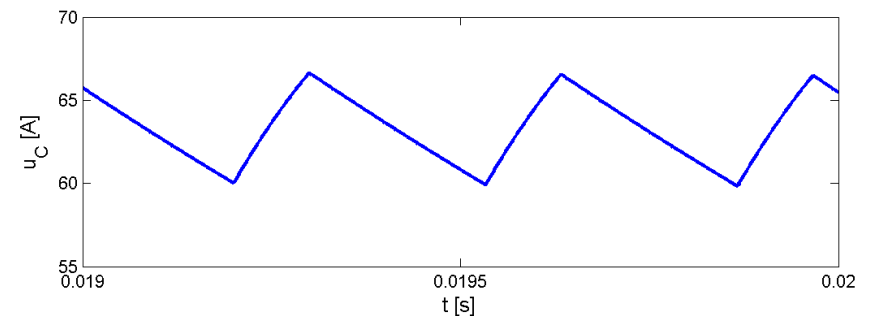
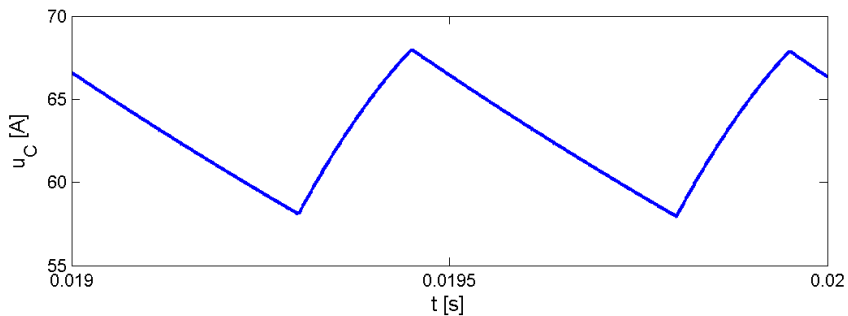
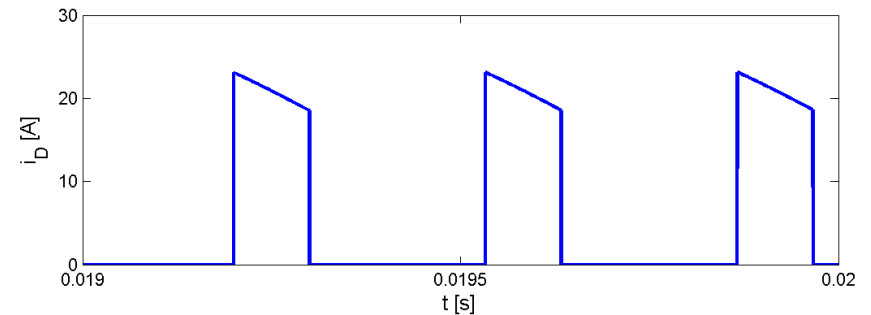
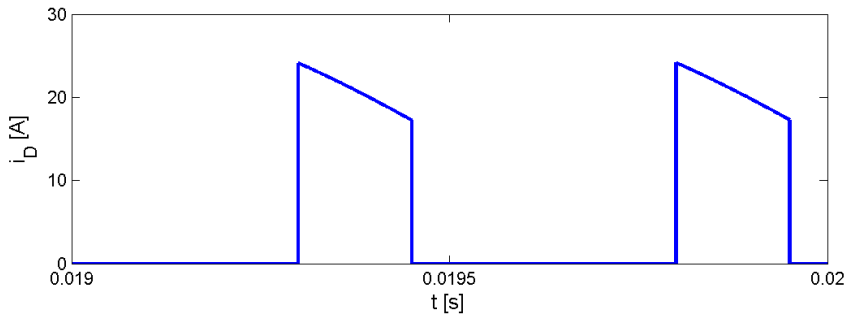
$$V_d = 20 \text{ V}$$

$$D = 0.7$$

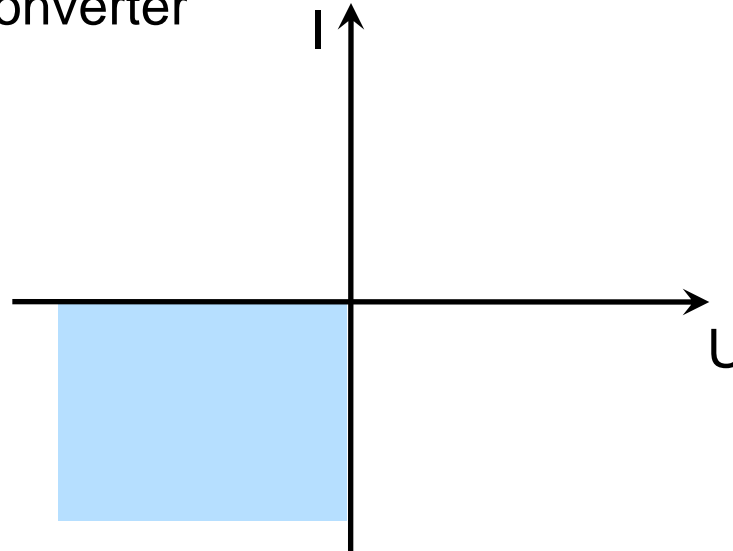


$f_s = 2 \text{ kHz}$

$f_s = 3 \text{ kHz}$



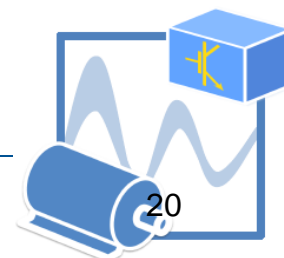
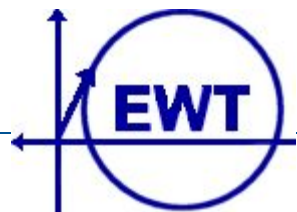
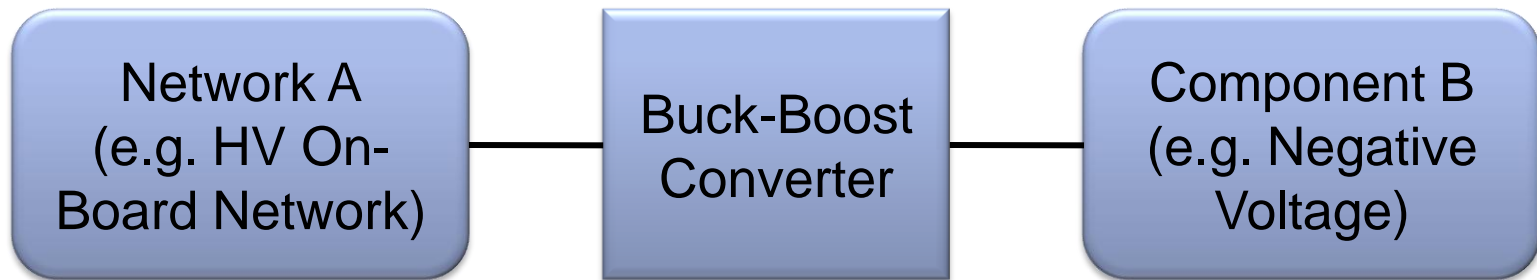
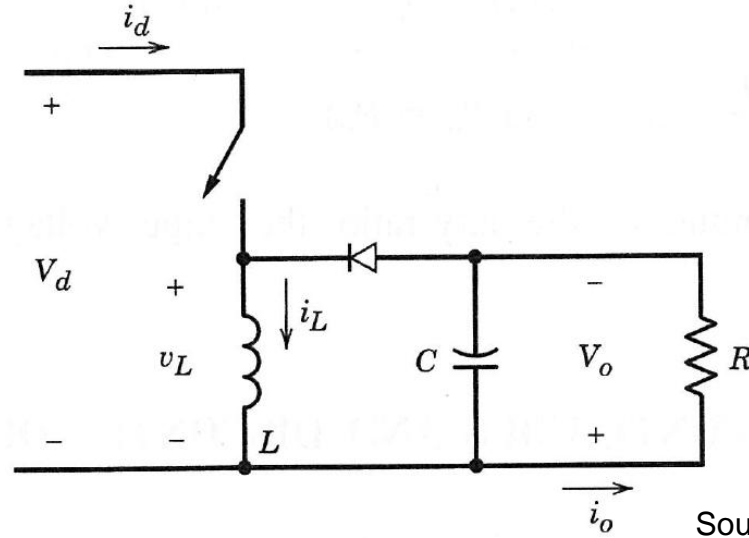
One-Quadrant Converter



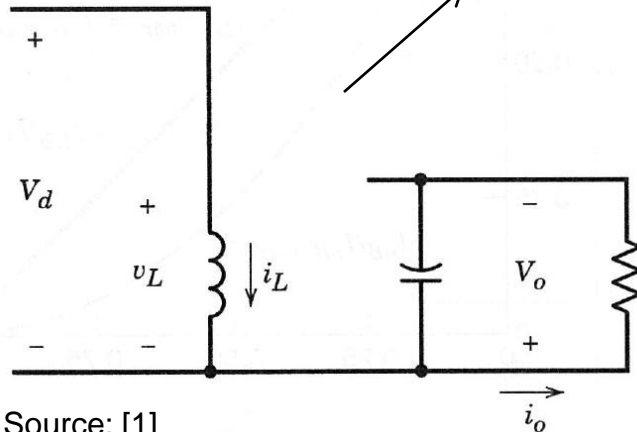
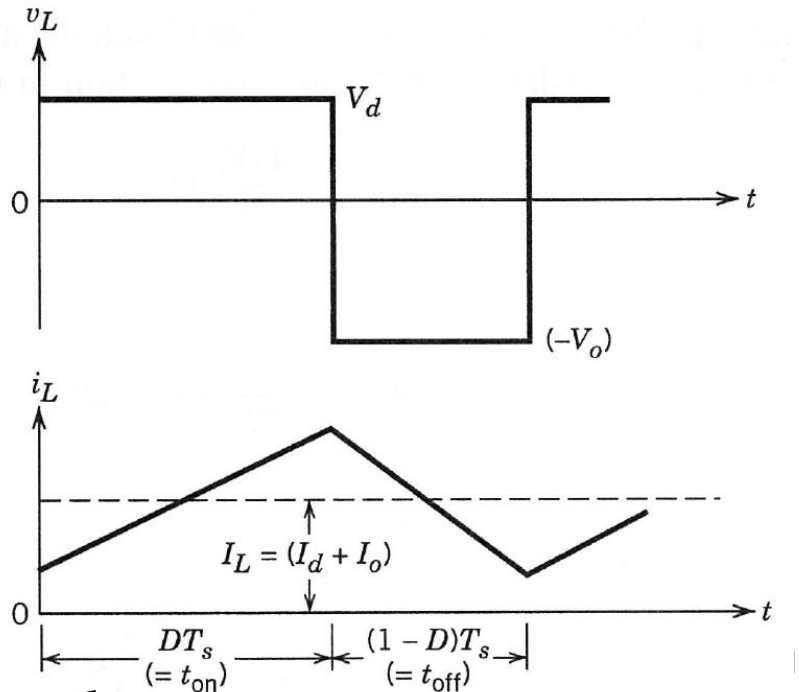
Fields of Application:

- Voltage Inversion
- Connecting Components to a Lower/Higher Voltage On-Board Network

Buck-Boost Converter – Principle Circuit



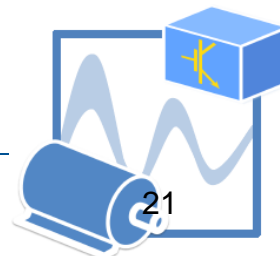
Buck-Boost Converter – Switching States



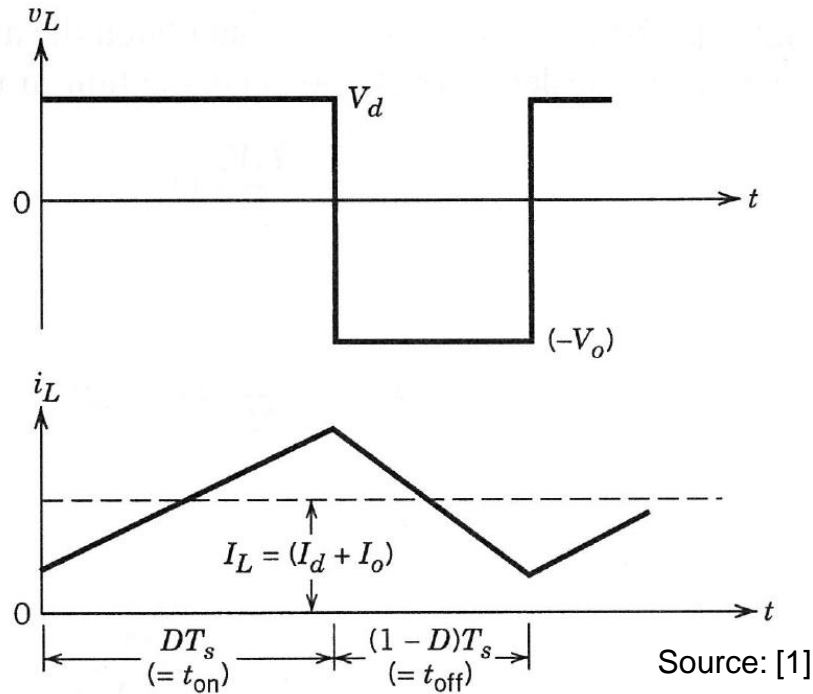
$$i_L(t) = I_{S,Bo} + \frac{V_d}{L} \cdot t$$

Source: [1]

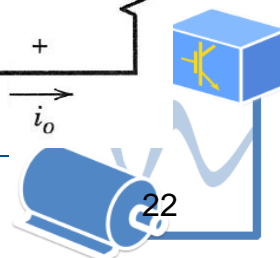
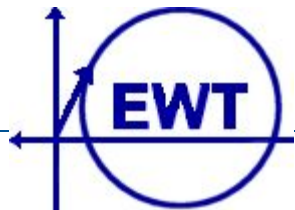
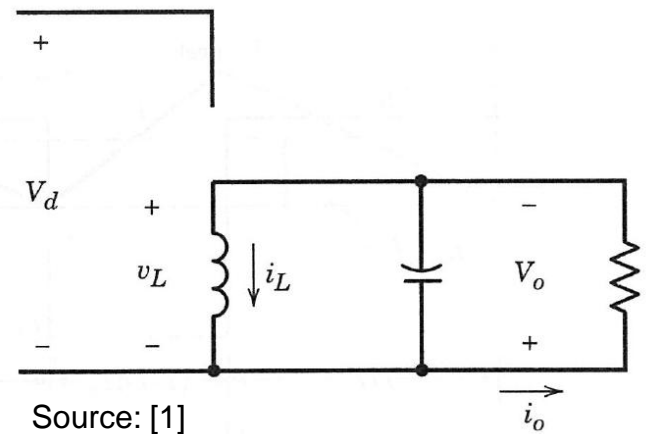
EV...

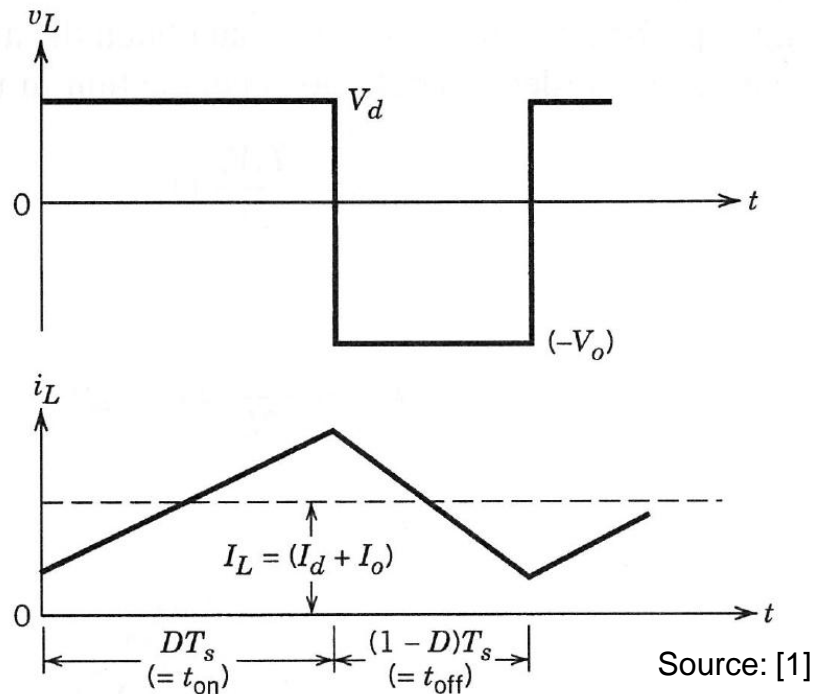


Buck-Boost Converter – Switching States



$$i_L(t) = I_{S,U_p} + \frac{(-V_0)}{L} \cdot t$$

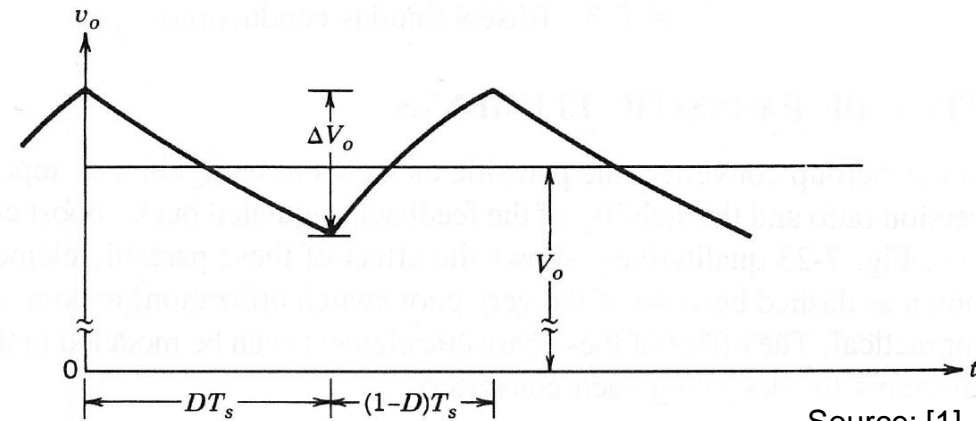
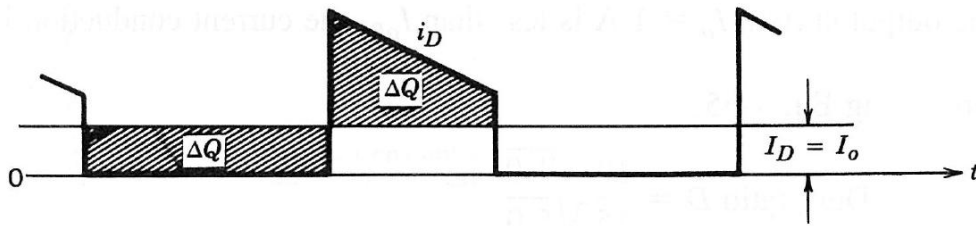




Steady-State: $V_d \cdot D \cdot T_s + (-V_0) \cdot (1 - D) \cdot T_s = 0$

$$\frac{V_0}{V_d} = \frac{D}{1 - D}$$

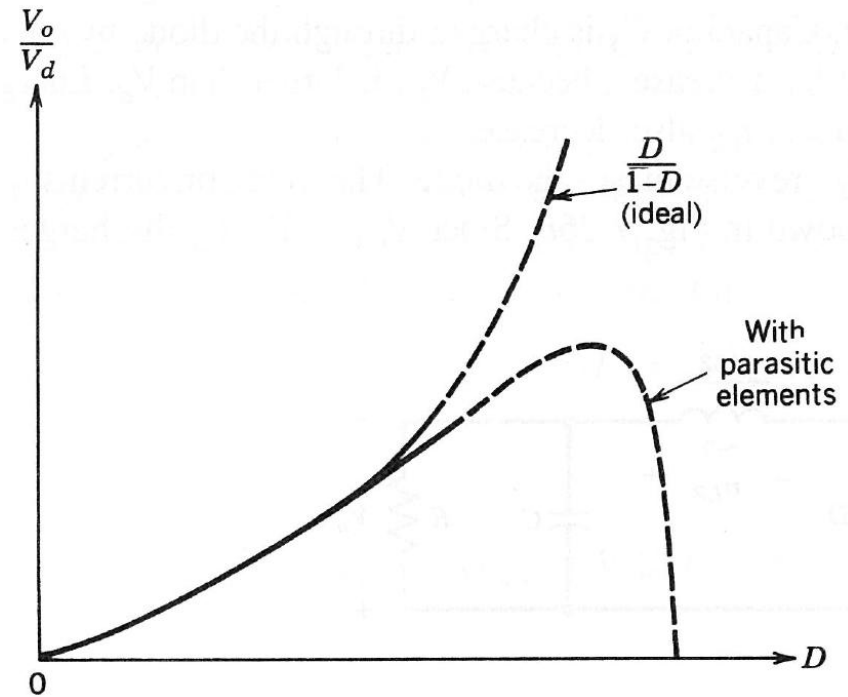
Buck-Boost Converter – Output Voltage



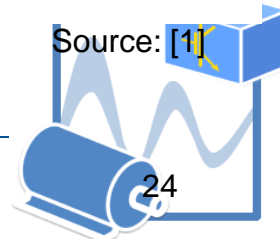
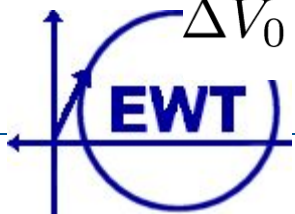
Source: [1]

$$\Delta V_o = \frac{\Delta Q}{C} = \frac{I_o \cdot D \cdot T_s}{C}$$

$$\Delta V_o = \frac{V_o}{R} \cdot \frac{D \cdot T_s}{C}$$



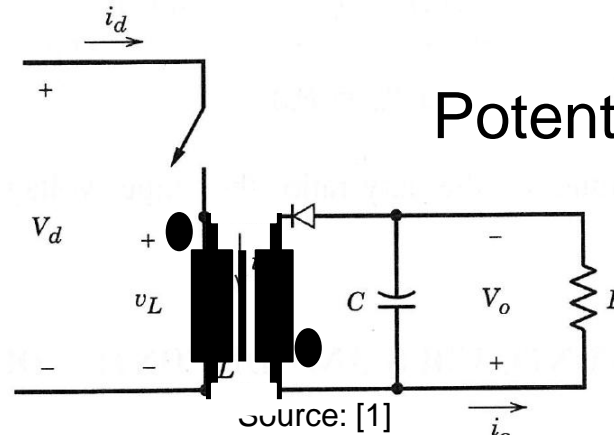
Source: [1]



Buck-Boost Converter – Simulation Results

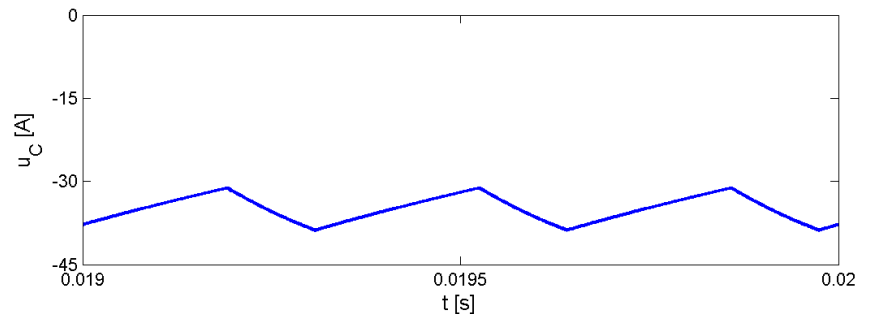
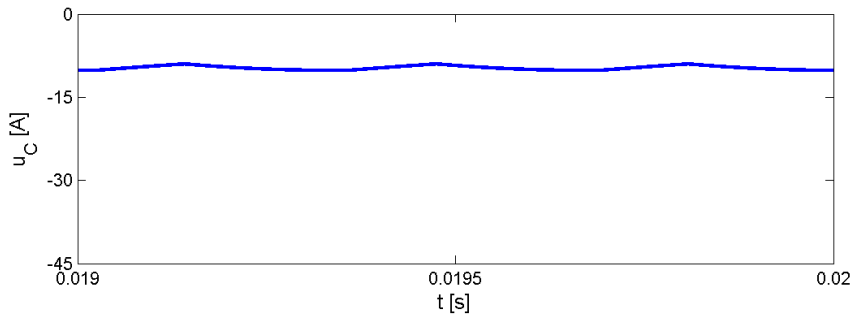
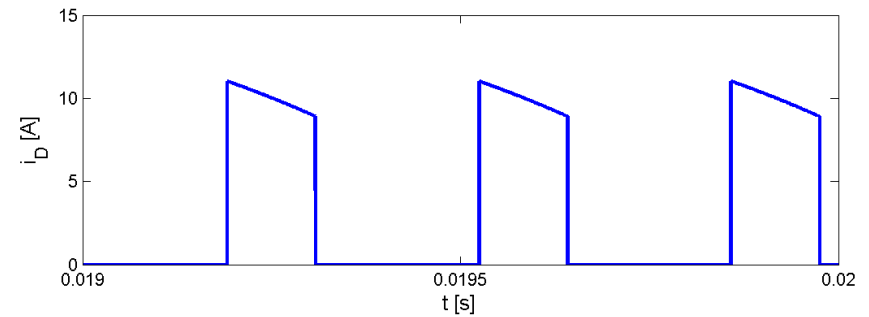
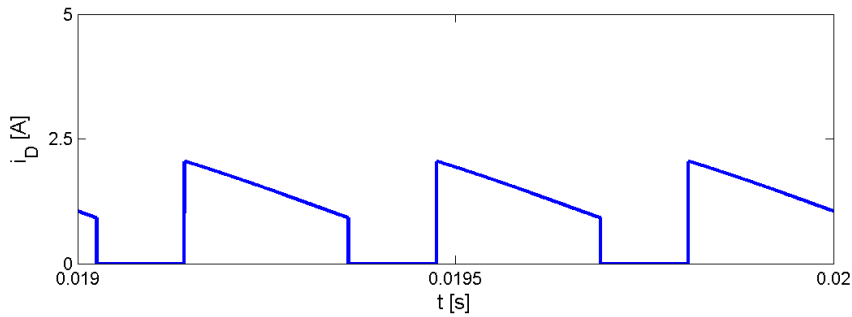
$$V_d = 20 \text{ V}$$

$$f_s = 3 \text{ kHz}$$

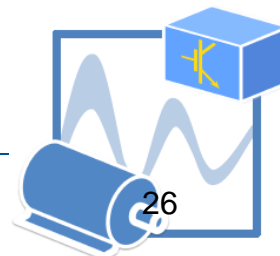
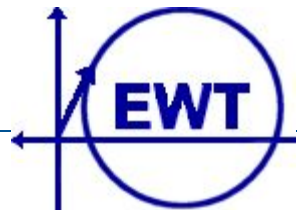
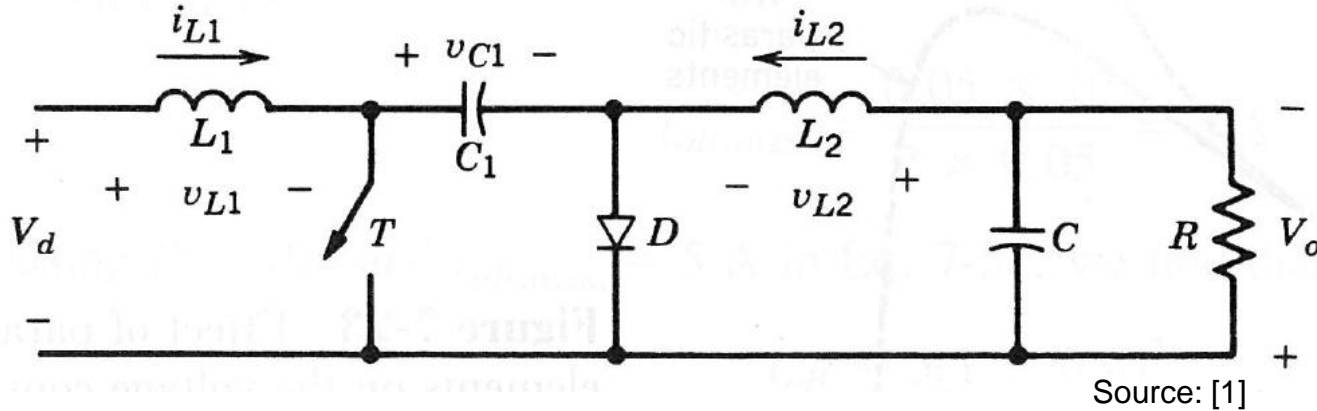


$D = 0.35$

$D = 0.65$



Cuk Converter – Principle Circuit



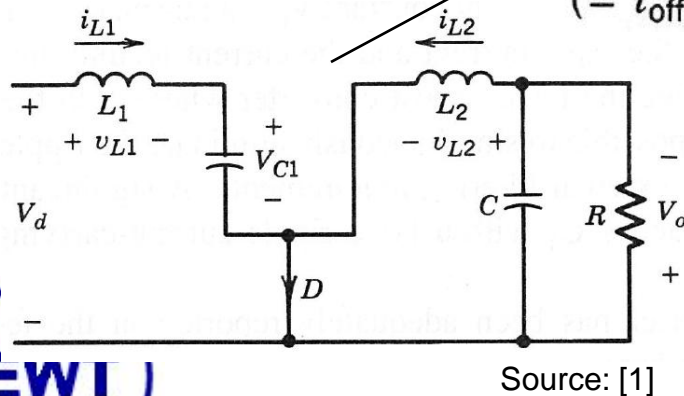
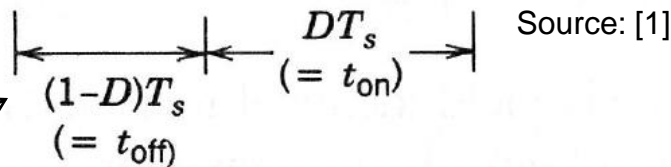
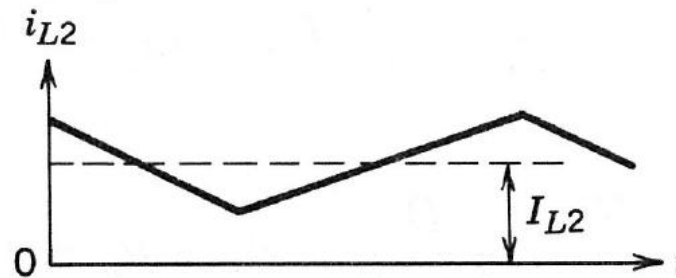
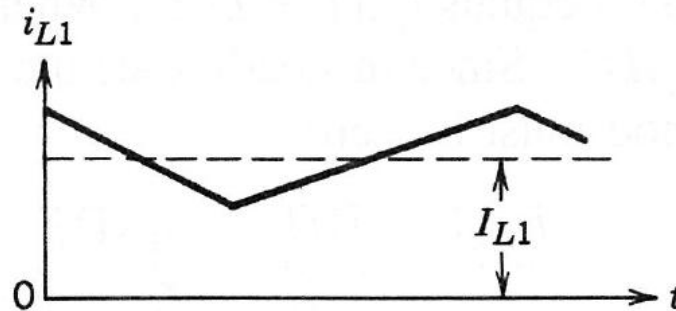
Cuk Converter – Switching States

Assumption:

$$V_{C1} = \text{const}$$

→ C_1 big enough

$$V_{C1} = V_d + V_o$$



Diode D conducting

- i_{L1} und i_{L2} flow through D
- i_{L1} charges C_1
- i_{L2} delivers Output Current
- i_{L1} and i_{L2} decrease

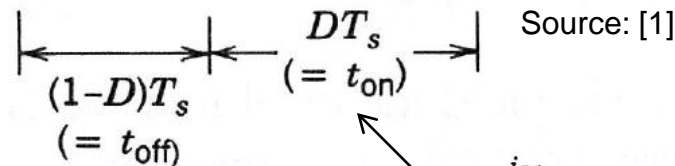
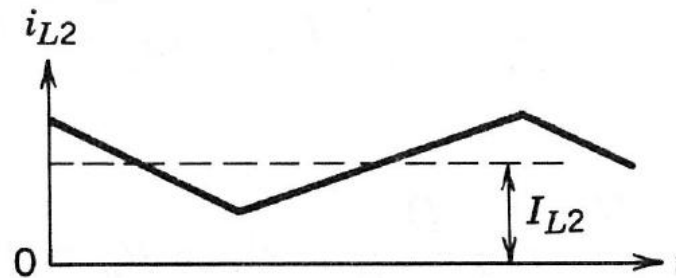
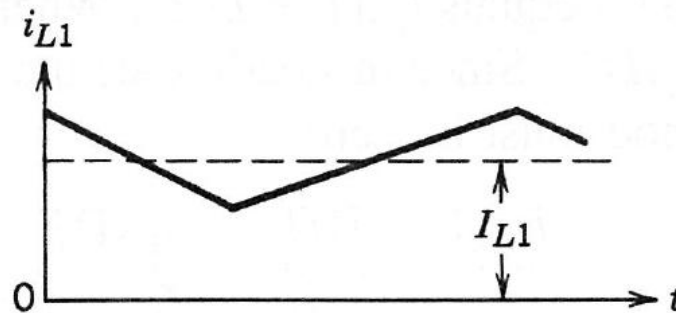
Cuk Converter – Switching States

Assumption:

$$V_{C1} = \text{const}$$

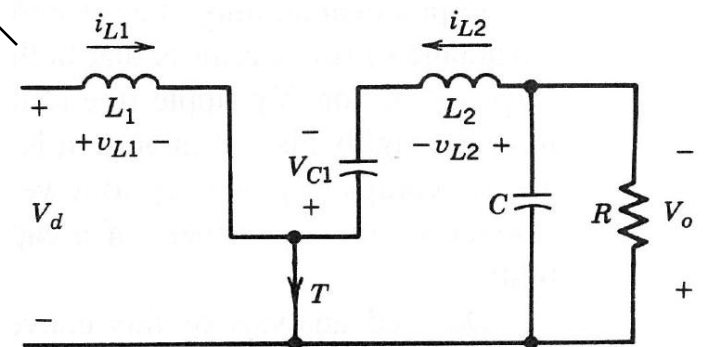
→ C_1 big enough

$$V_{C1} = V_d + V_o$$

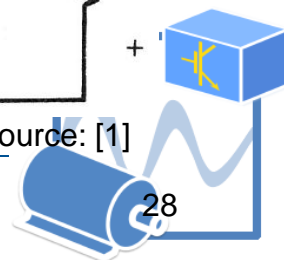
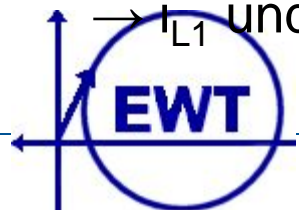


Switch T conducting

- i_{L1} and i_{L2} flow through T
- C_1 delivers Energy to Output and L_2
- Energy in L_1 rises
- i_{L1} und i_{L2} increase



Source: [1]



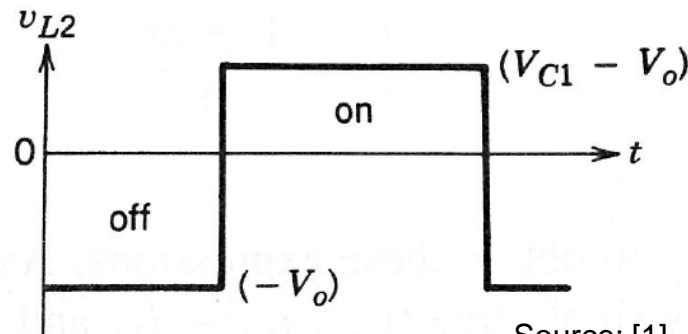
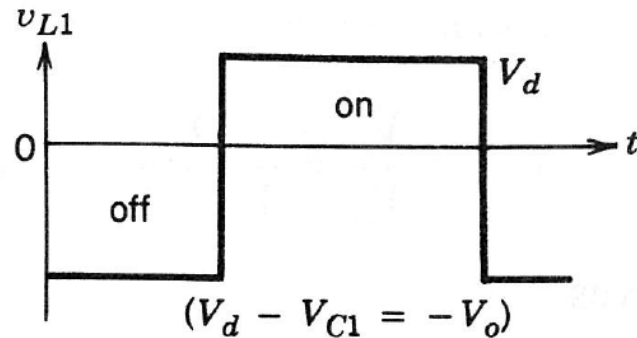
Cuk Converter – Output Voltage

Assumption:

$$V_{C1} = \text{const}$$

→ C_1 big enough

$$V_{C1} = V_d + V_o$$



Source: [1]

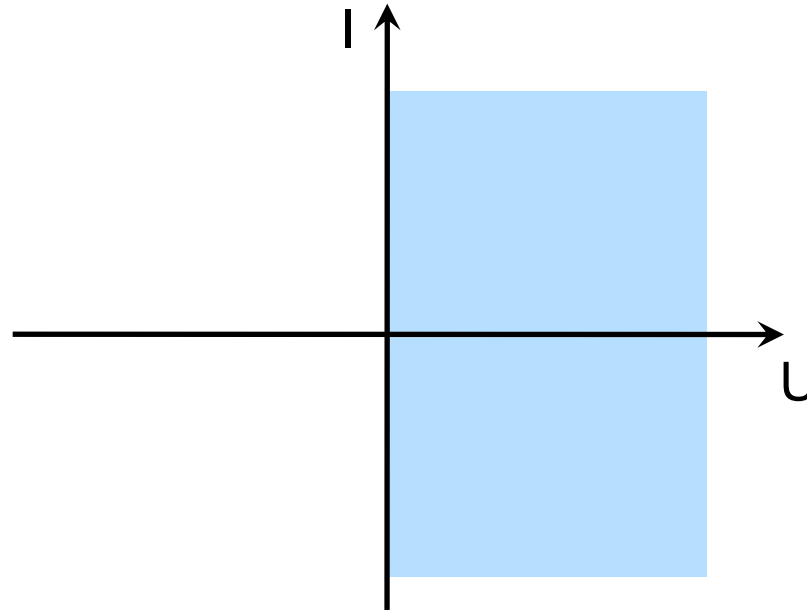
$$V_d \cdot D \cdot T_s + (V_d - V_{C1})(1 - D) \cdot T_s = 0$$

$$V_{C1} = \frac{1}{1 - D} \cdot V_d$$

$$(V_{C1} - V_o) \cdot D \cdot T_s + (-V_o)(1 - D) \cdot T_s = 0$$

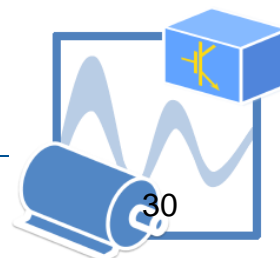
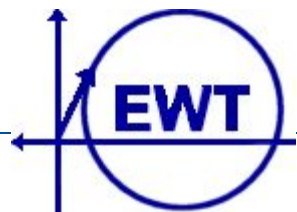
$$V_{C1} = \frac{1}{D} \cdot V_o$$

$$\frac{V_o}{V_d} = \frac{D}{1 - D}$$



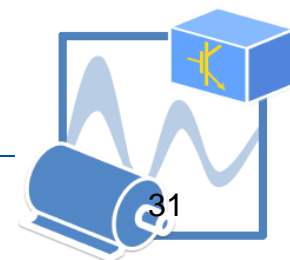
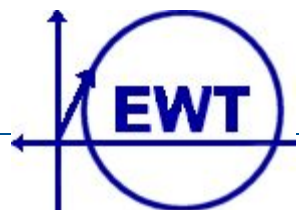
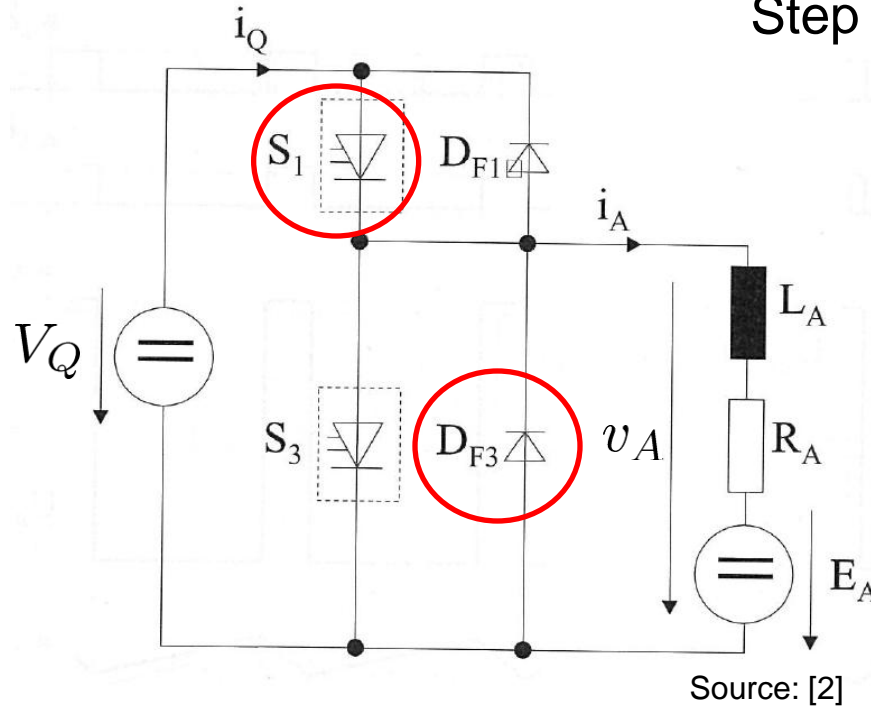
Fields of Application:

- Bidirectional Coupling of Two On-Board Networks
- Connecting Components with Lower Voltage Level to a Higher Voltage On-Board Network
- Current Inversion
- **Step Up-Step Down Converter**



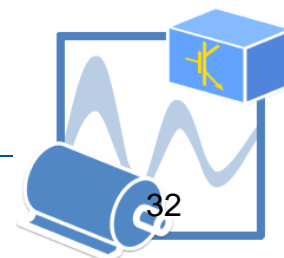
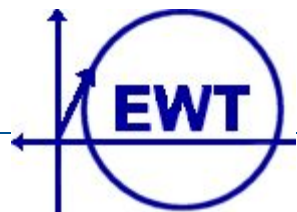
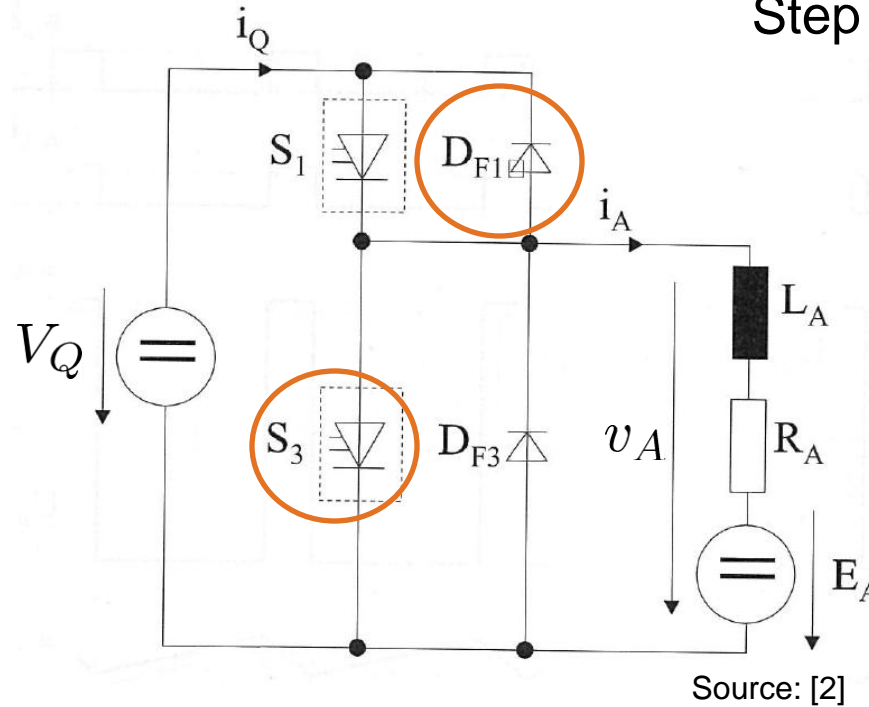
Two-Quadrant Converters – Principle Circuit

Step Down Mode



Two-Quadrant Converters – Principle Circuit

Step Up Mode

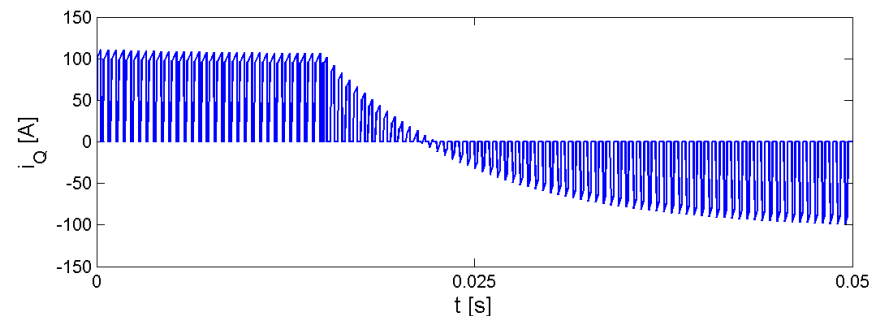
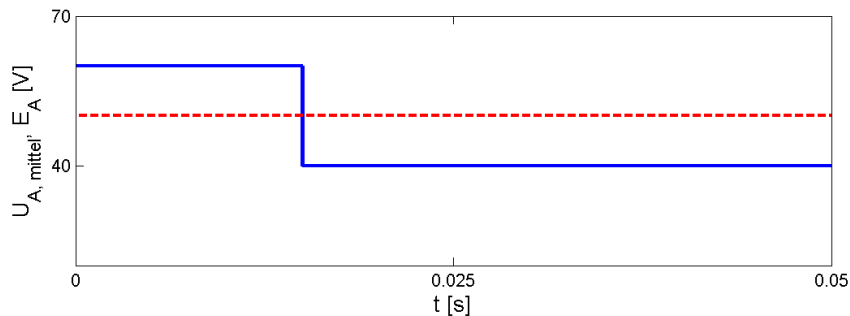
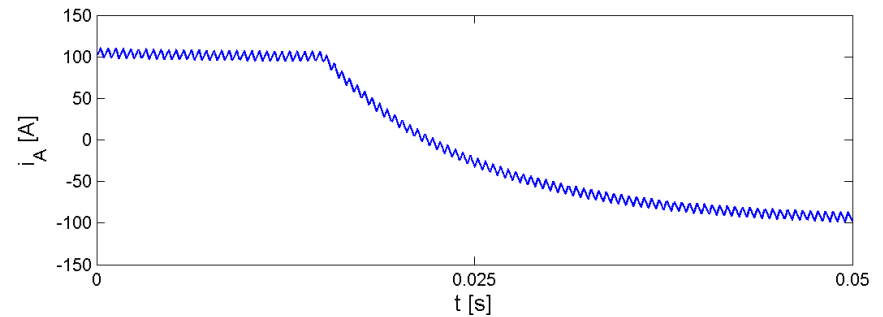
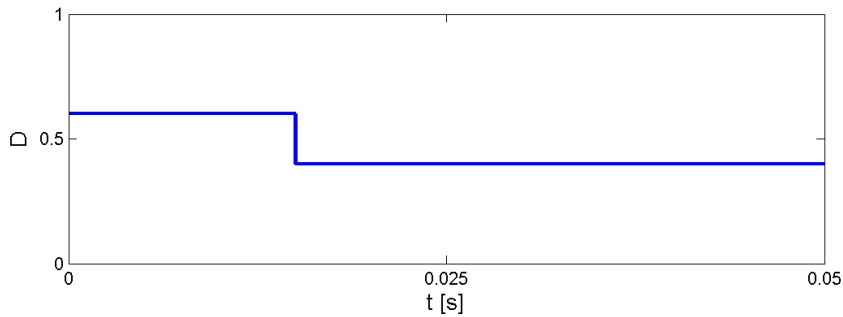
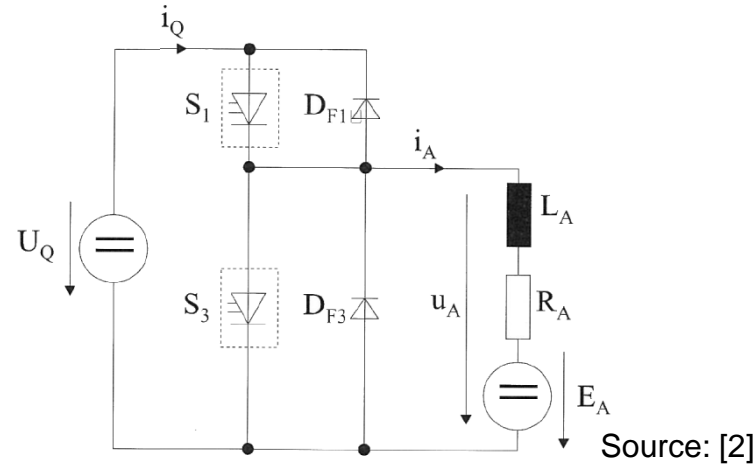


Step Down/Step Up Converter – Simulation

$$V_Q = 100 \text{ V}$$

$$E_A = 50 \text{ V}$$

$$f_s = 2 \text{ kHz}$$

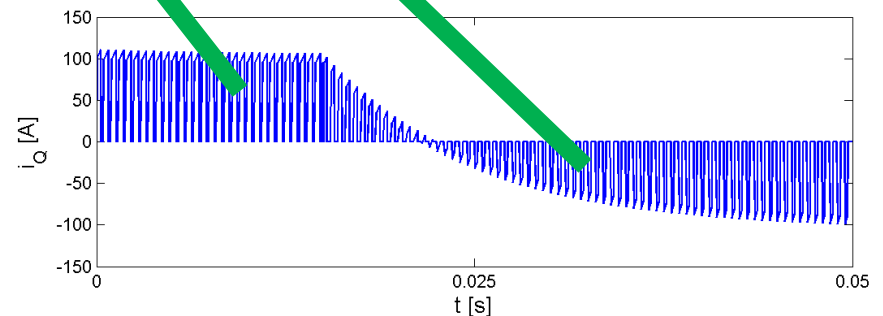
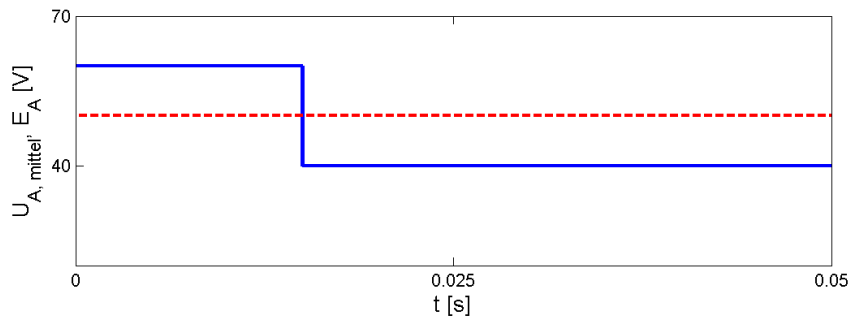
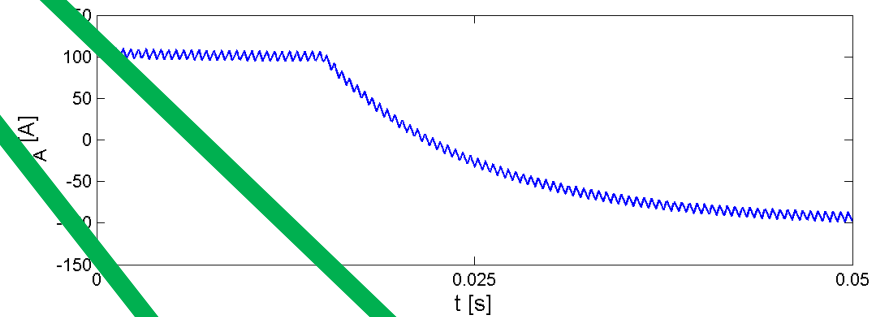
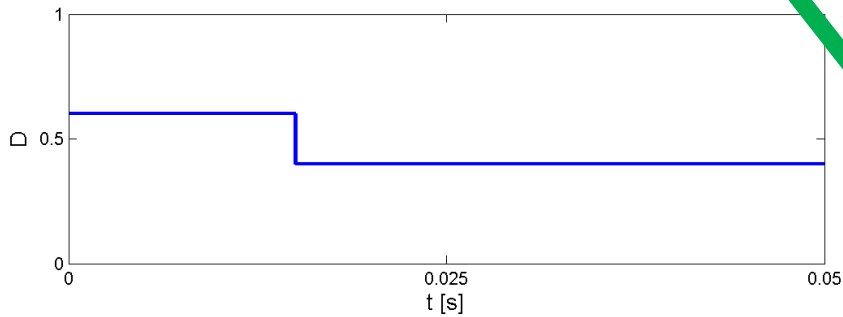
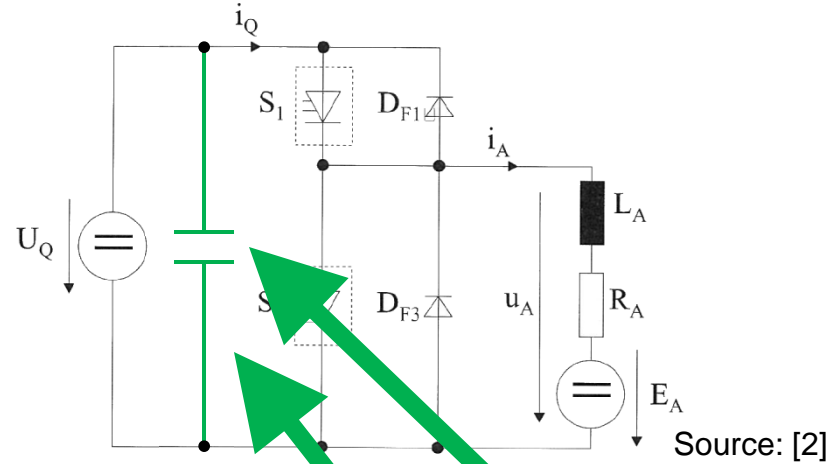


Step Down/Step Up Converter – Simulation

$$V_Q = 100 \text{ V}$$

$$E_A = 50 \text{ V}$$

$$f_s = 2 \text{ kHz}$$



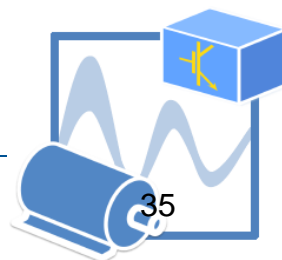
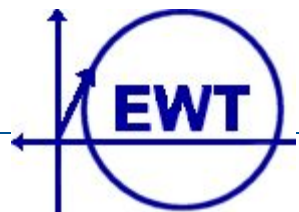
Limited at High Power because of

- Slow Switching of Large Semiconductor Devices
- Large Smoothing Inductances (due to High Current)
- High Ripple Current Stress in Smoothing Capacitor

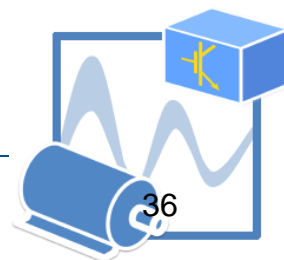
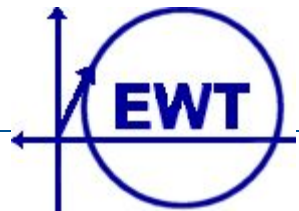
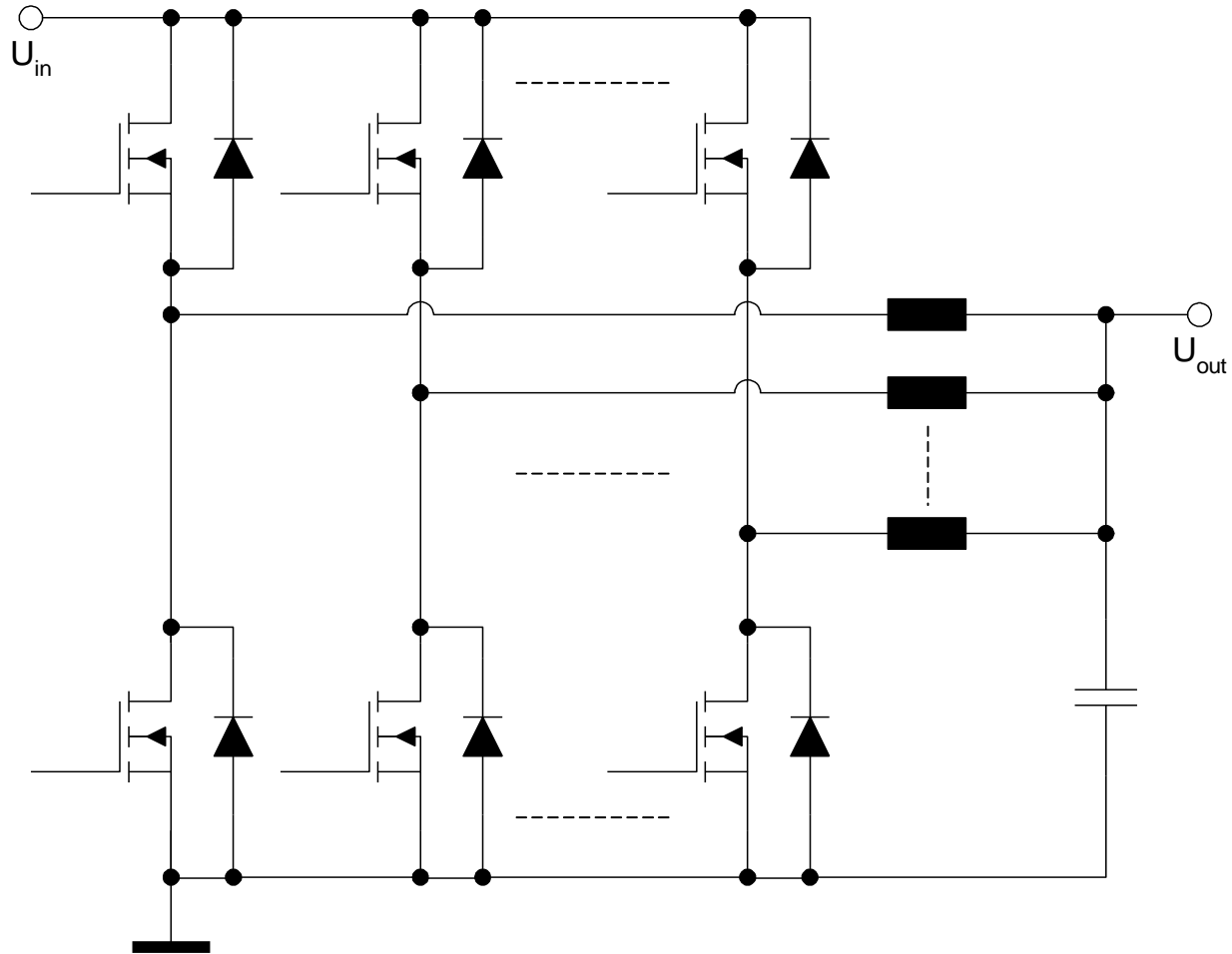
Cost-Intensive Passive Components

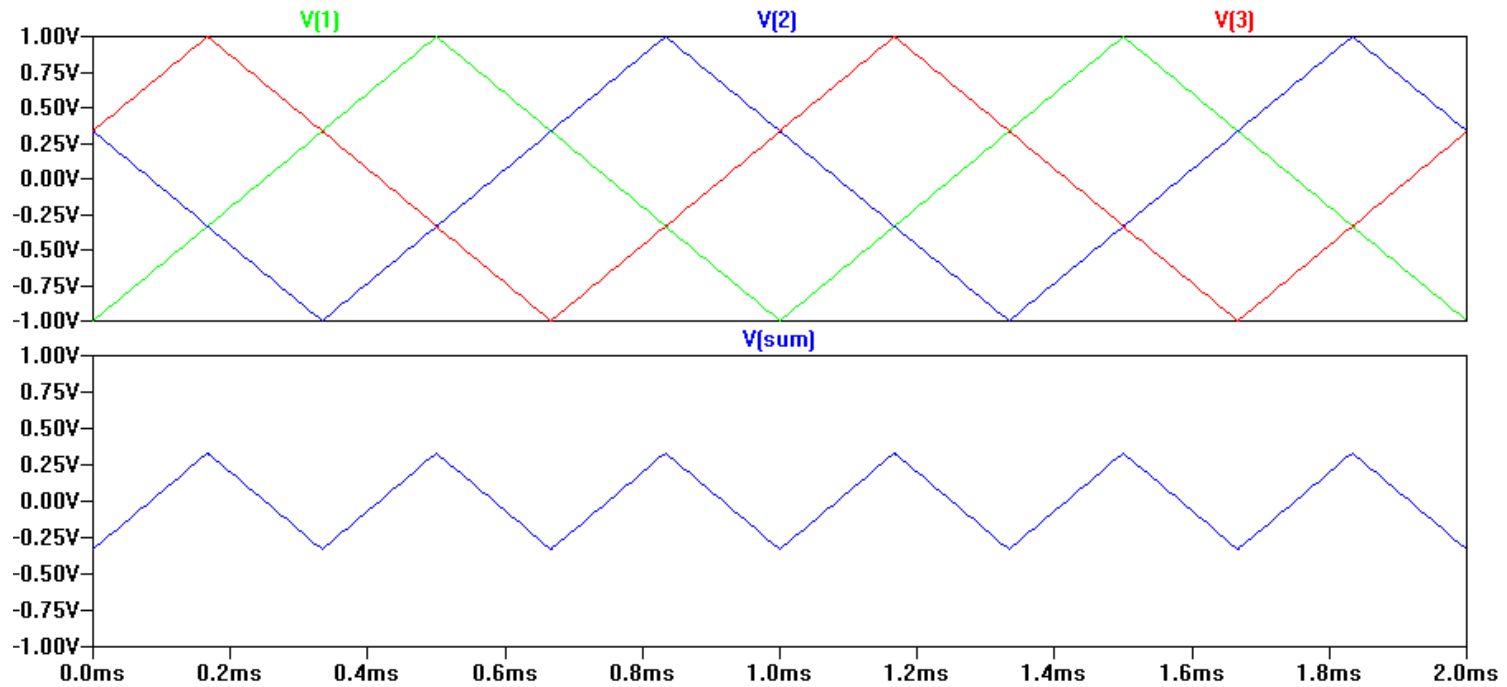
→ „Silicon instead of Passives“

→ Multi-phase DC/DC Converter

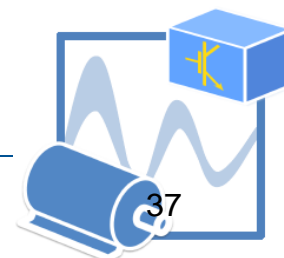
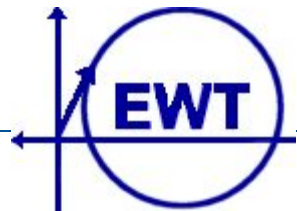


Half-Bridge – Multi-Phase Approach





Ripple-Current Superposition of Individual Phases



Advantages:

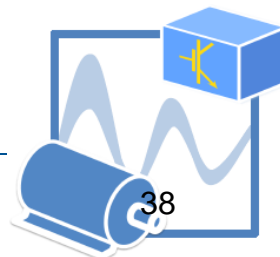
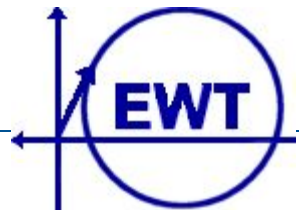
- + Less Current per Phase
- + Higher Modulation Frequency
- + Higher Effective Modulation Frequency by Phase-Shift in PWM Triggering
- Compact and Cheap Set-Up
- + Modular Design possible

Disadvantages:

- Risk of Ring Currents
- Asymmetrical Phase Currents

Balancing Alternatives:

- Series Resistors
- Central Control
- Master-Slave Approaches
- Magnetically Coupled Coils
- Fuzzy Logic



Ohmic Losses:

$$P_{\Omega} = R \cdot I_{out}^2$$

Switching Losses:

$$P_S = 1/2 \cdot V_{out} \cdot I_{out} \cdot (t_1 + t_2) \cdot f_S$$

On-State Power Losses Transistor:

$$P_{rdson} = R_{ds} \cdot I_{in}^2$$

Gate-Triggering:

$$P_{gate} = Q_{gate} \cdot V_{gs} \cdot f_S$$

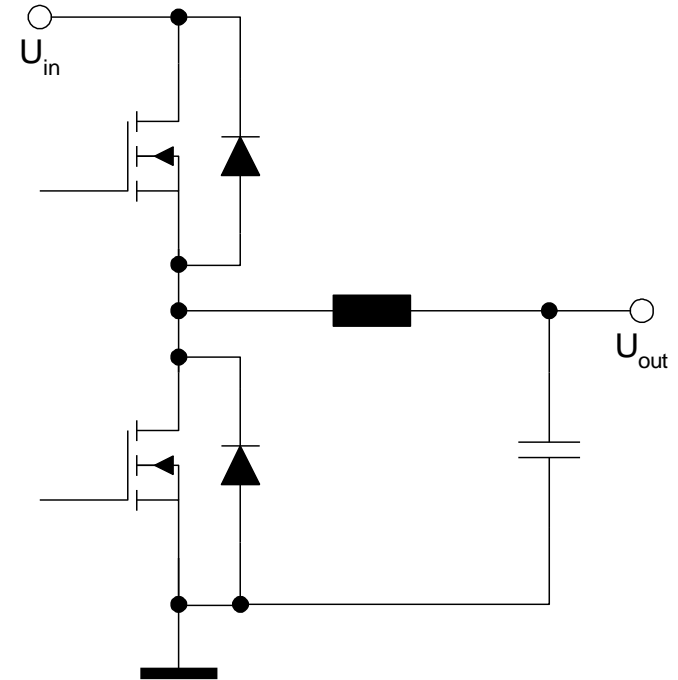
On-State Power Losses Diode:

$$P_d = V_d \cdot I_{out} + R_d \cdot I_{out}^2$$

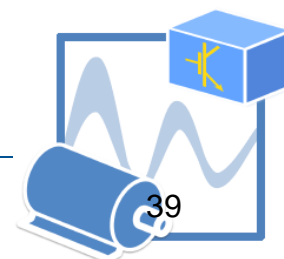
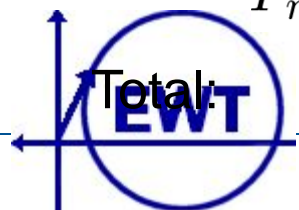
Reverse Recovery Diode:

$$P_{rr} = (I_{out} \cdot t_{rr} + Q_{rr}) \cdot V_{in} \cdot f_S$$

Total: $P_{\Sigma} = P_{\Omega} + P_S + P_{rdson} + P_{gate} + P_d + P_{rr}$



Example: 2Q Converter



- [1] N. Mohan, T. Undeland, W. Robbins,
„Power Electronics – Converters, Applications, and Design“,
3rd Edition, Wiley, 2003

- [2] D. Schröder,
„Leistungselektronische Schaltungen – Funktion, Auslegung und
Anwendung“,
2. Auflage, Springer, 2008

